

# CS450 - Structure of Higher Level Languages

## Metalinguistic Abstraction

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# Programming Languages Are Means to Model Complex Problems

- To design a complex system (of any kind) we need several general techniques:
- Combine primitive elements to form compound objects
- Abstract compound objects to form higher-level building blocks
- Preserve modularity by adopting appropriate large-scale views of system structure.
- We have used scheme for this purpose, but as our problems become more complex, we may need to resort to new languages that help us express new ideas more effectively.

# Metalinguistic Abstraction

- **Metalinguistic abstraction**, establishing new languages, plays an important role in all branches of engineering design.
- It is particularly important to computer programming – we can formulate new languages, and we can also implement these languages by constructing evaluators.
- An evaluator (or interpreter) for a programming language is a procedure that, when applied to an expression of the language, performs the actions required to evaluate that expression.
- It is **very** important to remember that the evaluator, which determines the meaning of expressions in a programming language, is just another program.

# Metalinguistic Abstraction

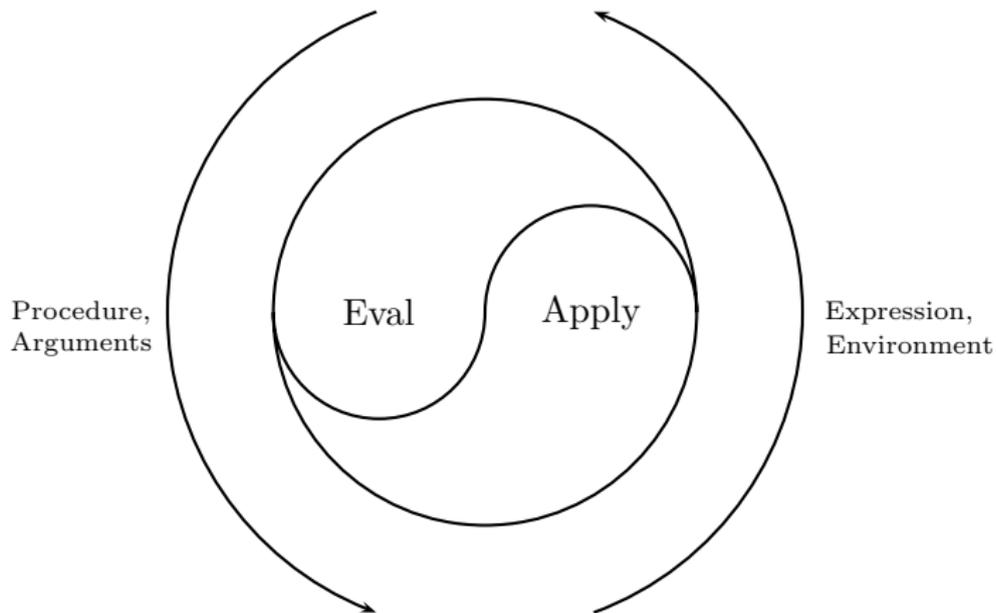
- As a matter of fact, we can think of any program as a "mini-language".
- The complex number package we mentioned earlier is the core of a language that deals with complex numbers, their representations and math operations, using primitives and building higher-level abstractions.
- We can also think of the RSA system in HW3 this way...
- There are several other examples in the book – a digital logic simulator, a polynomial manipulation system etc.

# Metalinguistic Abstraction

- In what follows we will use scheme to explore the ability of languages to build other languages.
- We will implement evaluators as procedures.
- Lisp is especially suitable due to its ability to represent and manipulate symbolic expressions.
- We will build an evaluator for Lisp itself.
- The evaluator is a subset of the Scheme language used in the text.
- It is rather simple, yet capable of executing most of the programs in the text...

# The Core of the Evaluator: Eval/Apply

The evaluation process can be described as the interplay between two procedures: `eval` and `apply`.



- Eval takes as arguments an expression and an environment.
- It classifies the expression and directs its evaluation.
- Eval is structured as a case analysis of the syntactic type of the expression to be evaluated.
- We express the determination of the type of an expression abstractly, making no commitment to any particular representation for the various types of expressions.
- The way we implement it allows us to change the syntax of the language by using the same evaluator, but with a different collection of syntax procedures.

- **Primitive expressions:**

- Self evaluating objects (like numbers), are evaluated to themselves.
- For variables, look up in the environment to find their values.

- **Special forms:**

- Quoted expressions are evaluated to the expression that was quoted.
- An assignment to (or a definition of) a variable recursively calls `eval` to compute the new value to be associated with the variable. The environment is modified accordingly.
- An `if` expression requires special processing of its parts, so as to evaluate the consequent if the predicate is true, or the alternative otherwise.

- **Special forms:** (cont.)

- A `lambda` expression must be transformed into an applicable procedure by packaging together the parameters and body with the environment of the evaluation.
- A `begin` expression requires evaluating its sequence of expressions in the order in which they appear.
- A `cond` is transformed into a nested `if` and evaluated.

- **Combinations:**

- For a procedure application, `eval` must recursively evaluate the operator part and the operands of the combination.
- The resulting procedure and arguments are passed to `apply`, which handles the actual procedure application.

# Definition of Eval (in text)

```
(define (eval exp env)
  (cond ((self-evaluating? exp) exp)
        ((variable? exp) (lookup-variable-value exp env))
        ((quoted? exp) (text-of-quotation exp))
        ((assignment? exp) (eval-assignment exp env))
        ((definition? exp) (eval-definition exp env))
        ((if? exp) (eval-if exp env))
        ((lambda? exp)
         (make-procedure (lambda-parameters exp)
                          (lambda-body exp)
                          env))
        ((begin? exp)
         (eval-sequence (begin-actions exp) env))
        ((cond? exp) (eval (cond->if exp) env))
        ((application? exp)
         (apply (eval (operator exp) env)
                 (list-of-values (operands exp) env)))
        (else
         (error "Unknown expression type -- EVAL" exp))))
```

# Definition of Eval

- In most Lisp implementations, `eval` is implemented by dispatching on type.
- This allows more flexibility in adding new types of expressions.
- The way it is implemented here requires us to edit the definition of `eval` whenever we add a new type.
- For our purposes we will use a slightly different version (see handout).

# Definition of Apply

- Apply takes two arguments, a procedure and a list of arguments to which the procedure should be applied.
- Apply classifies procedures into two kinds: It calls `apply-primitive-procedure` to apply primitives;
- Compound procedures are applied by sequentially evaluating the expressions that make up the body of the procedure.
- The environment for the evaluation of the body of a compound procedure is constructed by extending the base environment carried by the procedure to include a frame that binds the parameters of the procedure to the arguments to which the procedure is to be applied.

# Definition of Apply (in text)

```
(define (apply procedure arguments)
  (cond ((primitive-procedure? procedure)
        (apply-primitive-procedure procedure arguments))
        ((compound-procedure? procedure)
         (eval-sequence
          (procedure-body procedure)
          (extend-environment
           (procedure-parameters procedure)
           arguments
           (procedure-environment procedure))))
        (else
         (error
          "Unknown procedure type -- APPLY" procedure))))
```

# The CS450 Implementation

- In HW6: Special forms to be stored in a 1-D lookup table, like the one we saw earlier on.
- The table is wrapped up in a "dispatch on type" procedure (that's not called dispatch!), which supports insert, lookup and display.
- The `eval` implementation, named `xeval`, uses the table to look up special forms.
- We use tagged data (remember that?) to represent different kinds of expressions (same as the text).

# The CS450 Implementation

The values of the operands of an expression are being evaluated in sequence.

```
(define (list-of-values exps env)
  (if (no-operands? exps)
      '()
      (cons (xeval (first-operand exps) env)
            (list-of-values (rest-operands exps) env))))
```

```
define (eval-if exp env)
  (if (true? (xeval (if-predicate exp) env))
      (xeval (if-consequent exp) env)
      (xeval (if-alternative exp) env)))
```

# Evaluating Different Expressions

```
((define (eval-sequence exps env)
  (cond ((last-exp? exps) (xeval (first-exp exps) env))
        (else (xeval (first-exp exps) env)
                (eval-sequence (rest-exps exps) env))))
```

```
(define (eval-assignment exp env)
  (let ((name (assignment-variable exp)))
    (set-variable-value! name
      (xeval (assignment-value exp) env)
      env)
    name))    ;; A & S return 'ok
```

```
(define (eval-definition exp env)
  (let ((name (definition-variable exp)))
    (define-variable! name
      (xeval (definition-value exp) env)
      env)
    name))    ;; A & S return 'ok
```

# Representing Expressions

```
(define (self-evaluating? exp)
  (or (number? exp)
      (string? exp)
      (boolean? exp) ))
```

```
(define (variable? exp) (symbol? exp))
```

```
(define (quoted? exp)
  (tagged-list? exp 'quote))
```

```
(define (text-of-quotation exp) (cadr exp))
```

```
(define (tagged-list? exp tag)
  (if (pair? exp)
      (eq? (car exp) tag)
      #f))
```

# Representing Assignments

```
(define (assignment? exp)
  (tagged-list? exp 'set!))
```

```
(define (assignment-variable exp) (cadr exp))
```

```
(define (assignment-value exp) (caddr exp))
```

# Representing Definitions

```
(define (definition? exp)
  (tagged-list? exp 'define))
```

```
(define (definition-variable exp)
  (if (symbol? (cadr exp))
      (cadr exp)
      (caadr exp)))
```

```
(define (definition-value exp)
  (if (symbol? (cadr exp))
      (caddr exp)
      (make-lambda (cdadr exp)
                    (caddr exp))))
```

# Representing Definitions

- A definition can either be  
`(define <var> <value>)`  
or  
`(define (<var> <par_1> ... <par_n>) <body>)`
- In the second case, the variable is the `caadr` of the expression (the name of the function)
- The value in this case is turned into a lambda expression.
- `(cdadr exp)` is the list of parameters.
- `(cddr exp)` is the body.

# Representing Lambda Expressions

```
(define (lambda? exp) (tagged-list? exp 'lambda))
```

```
(define (lambda-parameters exp) (cadr exp))
```

```
(define (lambda-body exp) (cddr exp))
```

```
(define (make-lambda parameters body)
```

```
  (cons 'lambda (cons parameters body)))
```

Notice that the list must have at least one other element (except the tag lambda).

# Representing If Statements

```
(define (if? exp) (tagged-list? exp 'if))
```

```
(define (if-predicate exp) (cadr exp))
```

```
(define (if-consequent exp) (caddr exp))
```

```
(define (if-alternative exp)
  (if (not (null? (cddddr exp)))
      (cddddr exp)
      #f))
```

```
(define (make-if predicate consequent alternative)
  (list 'if predicate consequent alternative))
```

# Representing Sequences

```
(define (begin? exp) (tagged-list? exp 'begin))
```

```
(define (begin-actions exp) (cdr exp))
```

```
(define (last-exp? seq) (null? (cdr seq)))
```

```
(define (first-exp seq) (car seq))
```

```
(define (rest-exps seq) (cdr seq))
```

```
(define (sequence->exp seq)
```

```
  (cond ((null? seq) seq)
```

```
        ((last-exp? seq) (first-exp seq))
```

```
        (else (make-begin seq))))
```

```
(define (make-begin seq) (cons 'begin seq))
```

# User Defined Procedures

Procedure applications – any compound expression that is not one of the above expression types.

```
(define (application? exp) (pair? exp))  
(define (operator exp) (car exp))  
(define (operands exp) (cdr exp))
```

```
(define (no-operands? ops) (null? ops))  
(define (first-operand ops) (car ops))  
(define (rest-operands ops) (cdr ops))
```

# Representing cond

Cond is syntactically transformed into a nest of if expressions.

```
(define (cond? exp) (tagged-list? exp 'cond))
```

```
(define (cond-clauses exp) (cdr exp))
```

```
(define (cond-else-clause? clause)  
  (eq? (cond-predicate clause) 'else))
```

```
(define (cond-predicate clause) (car clause))
```

```
(define (cond-actions clause) (cdr clause))
```

```
(define (cond->if exp)  
  (expand-clauses (cond-clauses exp)))
```

## Representing cond (Cont.)

```
(define (expand-clauses clauses)
  (if (null? clauses)
      #f ; no else clause -- return #f
      (let ((first (car clauses))
            (rest (cdr clauses)))
        (if (cond-else-clause? first)
            (if (null? rest)
                (sequence->exp (cond-actions first))
                (error "ELSE clause isn't last -- COND->IF "
                      clauses))
            (make-if (cond-predicate first)
                     (sequence->exp (cond-actions first))
                     (expand-clauses rest))))))
```

# Truth Values and Procedure Objects

```
(define (true? x)
  (not (eq? x #f)))
```

```
(define (false? x)
  (eq? x #f))
```

;;; Procedures

```
(define (make-procedure parameters body env)
  (list 'procedure parameters body env))
```

```
(define (user-defined-procedure? p)
  (tagged-list? p 'procedure))
```

```
(define (procedure-parameters p) (cadr p))
(define (procedure-body p) (caddr p))
(define (procedure-environment p) (cadddr p))
```

# Representing Environments

- An environment is a list of frames.
- The enclosing environment is the cdr of the current environment.
- Each frame is represented as a pair of lists:
  - ① a list of the variables bound in that frame, and
  - ② a list of the associated values.
- For HW6 it is **crucial** to understand how environments are represented.

# Representing Environments

```
(define (enclosing-environment env) (cdr env))

(define (first-frame env) (car env))

(define the-empty-environment '())

(define (make-frame variables values)
  (cons variables values))

(define (frame-variables frame) (car frame))
(define (frame-values frame) (cdr frame))

(define (add-binding-to-frame! var val frame)
  (set-car! frame (cons var (car frame)))
  (set-cdr! frame (cons val (cdr frame))))
```

# Extending an Environment

- Creating a new frame with a set of variables and values.
- Making the base environment the enclosing environment of the new frame.

```
(define (xtend-environment vars vals base-env)
  (if (= (length vars) (length vals))
      (cons (make-frame vars vals) base-env)
      (if (< (length vars) (length vals))
          (error "Too many arguments supplied " vars vals)
          (error "Too few arguments supplied " vars vals))))
```

# Looking up a Variable's Value

Scan current frame, if not found – go to the enclosing environment.

```
(define (lookup-variable-value var env)
  (define (env-loop env)
    (define (scan vars vals)
      (cond ((null? vars)
             (env-loop (enclosing-environment env)))
            ((eq? var (car vars))
             (car vals))
            (else (scan (cdr vars) (cdr vals)))))
    (if (eq? env the-empty-environment)
        (error "Unbound variable " var)
        (let ((frame (first-frame env)))
          (scan (frame-variables frame)
                (frame-values frame)))))
    (env-loop env))
```

## Set a Variable's Value

Change value first time it's found.

```
(define (set-variable-value! var val env)
  (define (env-loop env)
    (define (scan vars vals)
      (cond ((null? vars)
             (env-loop (enclosing-environment env)))
            ((eq? var (car vars))
             (set-car! vals val))
            (else (scan (cdr vars) (cdr vals)))))
    (if (eq? env the-empty-environment)
        (error "Unbound variable -- SET! " var)
        (let ((frame (first-frame env)))
          (scan (frame-variables frame)
                (frame-values frame)))))
  (env-loop env))
```

# Defining a Variable's Value

Add a binding to current frame, or change value if exists already.

```
(define (define-variable! var val env)
  (let ((frame (first-frame env)))
    (define (scan vars vals)
      (cond ((null? vars)
             (add-binding-to-frame! var val frame))
            ((eq? var (car vars))
             (set-car! vals val))
            (else (scan (cdr vars) (cdr vals))))))
    (scan (frame-variables frame)
          (frame-values frame))))
```

# Initial Environment Setup

- The global environment starts up as containing primitive procedures only.
- In HW6 you will need to modify that, and separate the primitive procedure installation from the initial setup.
- In the current setup there are only four primitive procedures installed.
- Think what it means for other primitive procedures... (hint for HW6).

# Initial Environment Setup

```
(define (setup-environment)
  (let ((initial-env
        (xtend-environment (primitive-procedure-names)
                           (primitive-procedure-objects)
                           the-empty-environment)))
    initial-env))

(define (primitive-procedure? proc)
  (tagged-list? proc 'primitive))

(define (primitive-implementation proc) (cadr proc))

(define primitive-procedures
  (list (list 'car car)
        (list 'cdr cdr)
        (list 'cons cons)
        (list 'null? null?))
  ;; more primitives
  ))
```

# Initial Environment Setup

```
(define (primitive-procedure-names)
  (map car
    primitive-procedures))
```

```
(define (primitive-procedure-objects)
  (map (lambda (proc) (list 'primitive (cadr proc)))
    primitive-procedures))
```

```
;;; Here is where we rely on the underlying Scheme
;;; implementation to know how to apply
;;; a primitive procedure.
```

```
(define (apply-primitive-procedure proc args)
  (apply (primitive-implementation proc) args))
```

# The Main Driver Loop

- read returns an internal representation of the next expression.
- It does not evaluate anything.
- xeval does the actual evaluation.

```
(define input-prompt "s450==> ")
```

```
(define (s450)
  (prompt-for-input input-prompt)
  (let ((input (read)))
    (let ((output (xeval input the-global-environment)))
      (user-print output)))
  (s450))
```

```
(define (prompt-for-input string)
  (newline) (newline) (display string))
```

# The Main Driver Loop

```
(define (user-print object)
  (if (user-defined-procedure? object)
      (display (list 'user-defined-procedure
                    (procedure-parameters object)
                    (procedure-body object)
                    '<procedure-env>))
      (display object)))

(define the-global-environment (setup-environment))

(display "... loaded the metacircular evaluator.
(s450) runs it.")
(newline)
```