

Figure 1: Graph of the Deterministic Finite Automaton \mathcal{M}

Homework 1

Due Wednesday, November 9 2011

1. Consider the dfa $\mathcal{M} = (\{a, b\}, \{q_0, q_1, q_2\}, \delta, q_0, \{q_1\})$ whose graph is given in Figure 1. Determine the language accepted by the automaton \mathcal{M} .
2. Construct deterministic finite automata that accept the following languages over the alphabet $A = \{a, b, c\}$:
 - (a) The set of all words that begin with ab and end with ba .
 - (b) The set $\{bab\}$.
 - (c) The set $A^* - \{bab\}$.
 - (d) The set of all words $x \in A^*$ that contain at least three as .
3. Each of these languages is a regular language over the alphabet $A = \{0, 1\}$. Draw the transition diagram of a deterministic finite automaton that accepts it.
 - (a) A^* .
 - (b) $\{\lambda\}$.
 - (c) \emptyset .
4. Let A be an alphabet. If b is a symbol such that $b \notin A$, construct a nondeterministic finite automaton that accepts the language A^*b .

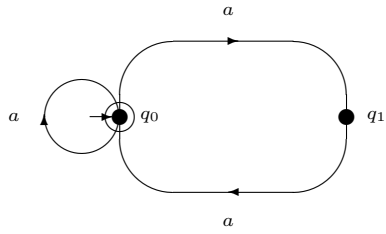


Figure 2: Graph of the Automaton \mathcal{M}

5. Let $\mathcal{M} = (A, Q, \delta, q_0, F)$ be a ndfa. Define $\phi(q, w, q')$ as the number of paths in the graph of \mathcal{M} from the state q to the state q' with label w . Prove that for the automaton $\mathcal{M} = (\{a, b\}, \{q_0, q_1\}, \delta, q_0, \{q_0\})$ whose graph is given in Figure 2 we have $\phi(q_0, a^n, q_0) = f_{n+1}$, where f_n is the n^{th} Fibonacci number and $n \geq 0$.