

Support Vector Machines - III

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Letter Image Recognition Data

Data was created by D. J. Slate and used in P. W. Frey and D. J. Slate (Machine Learning Vol 6 #2 March 91) "Letter Recognition Using Holland-style Adaptive Classifiers".

The Structure of Data

The objective is to identify each of a large number of black-and-white rectangular pixel displays as one of the 26 capital letters in the English alphabet.

- The character images were based on 20 different fonts and each letter within these 20 fonts was randomly distorted to produce a file of 20,000 unique stimuli.
- Each stimulus was converted into 16 primitive numerical attributes (statistical moments and edge counts) which were then scaled to fit into a range of integer values from 0 through 15.
- Training is made for the first 16000 items and then use the resulting model to predict the letter category for the remaining 4000.

Attribute Information

1.	lettr	capital letter	(26 values from A to Z)
2.	x-box	horizontal position of box	(integer)
3.	y-box	vertical position of box	(integer)
4.	width	width of box	(integer)
5.	high	height of box	(integer)
6.	onpix	total # on pixels	(integer)
7.	x-bar	mean x of on pixels in box	(integer)
8.	y-bar	mean y of on pixels in box	(integer)
9.	x2bar	mean x variance	(integer)
10.	y2bar	mean y variance	(integer)
11.	xybar	mean x y correlation	(integer)
12.	x2ybr	mean of $x * x * y$	(integer)
13.	xy2br	mean of $x * y * y$	(integer)
14.	x-ege	mean edge count left to right	(integer)
15.	xegvy	correlation of x-ege with y	(integer)
16.	y-ege	mean edge count bottom to top	(integer)
17.	yegvx	correlation of y-ege with x	(integer)

Class Distribution

789 A	766 B	736 C	805 D	768 E	775 F	773 G
734 H	755 I	747 J	739 K	761 L	792 M	783 N
753 O	803 P	783 Q	758 R	748 S	796 T	813 U
764 V	752 W	787 X	786 Y	734 Z		

Data Structure of the object letters

```
> letters <- read.csv("letter-recognition.csv",header=TRUE,sep=",")
> str(letters)
'data.frame': 20000 obs. of 17 variables:
 $ lettr : Factor with 26 levels "A","B","C","D",...: 20 9 4 14 7 19 2 1 10 13 ...
 $ x.box : int 2 5 4 7 2 4 4 1 2 11 ...
 $ y.box : int 8 12 11 11 1 11 2 1 2 15 ...
 $ width : int 3 3 6 6 3 5 5 3 4 13 ...
 $ high : int 5 7 8 6 1 8 4 2 4 9 ...
 $ onpix : int 1 2 6 3 1 3 4 1 2 7 ...
 $ x.bar : int 8 10 10 5 8 8 8 8 10 13 ...
 $ y.bar : int 13 5 6 9 6 8 7 2 6 2 ...
 $ x2bar : int 0 5 2 4 6 6 6 2 2 6 ...
 $ y2bar : int 6 4 6 6 6 9 6 2 6 2 ...
 $ xybar : int 6 13 10 4 6 5 7 8 12 12 ...
 $ x2ybr : int 10 3 3 4 5 6 6 2 4 1 ...
 $ xy2br : int 8 9 7 10 9 6 6 8 8 9 ...
 $ xletters.ede: int 0 2 3 6 1 0 2 1 1 8 ...
 $ xegvy : int 8 8 7 10 7 8 8 6 6 1 ...
 $ y.ege : int 0 4 3 2 5 9 7 2 1 1 ...
 $ yegvx : int 8 10 9 8 10 7 10 7 7 8 ...
```

R Packages specialized in SVMs:

- kernlab
- svmlight
- libsvm
- e1071

We shall use kernlab.


```
>  
> local(pkg <- select.list(sort(.packages(all.available = TRUE)),graphics=TRUE)  
+ if(nchar(pkg)) library(pkg, character.only=TRUE))  
Warning message:  
package kernlab was built under R version 3.0.2
```

Construction of Training Set and Test Set

```
>  
> letters_train ← letters[1:16000, ]  
> letters_test  ← letters[16001:20000, ]  
>
```

```
> letter_classifier <- ksvm(lettr ~ ., data= letters_train, kernel = "vanilladot")
Setting default kernel parameters
> letter_classifier
Support Vector Machine object of class "ksvm"
SV type: C-svc (classification)
parameter : cost C = 1
Linear (vanilla) kernel function.
Number of Support Vectors : 7037
Objective Function Value : -14.1746 -20.0072 -23.5628 -6.2009 -7.5524 -32.7694 -49.9786 -18.1824 -62.1111 -32.7
-16.2209 -32.2837 -28.9777 -51.2195 -13.276 -35.6217 -30.8612 -16.5256 -14.6811 -32.7475 -30.3219 -7.7956 -11.8
-32.3463 -13.1262 -9.2692 -153.1654 -52.9678 -76.7744 -119.2067
...
Training error : 0.130062
```

Other Available Kernels

- Gaussian radial basis function `rbfdot`, $K(\mathbf{x}, \mathbf{y}) = e^{-\sigma \|\mathbf{x} - \mathbf{y}\|}$;
- the polynomial kernel `polydot` defined as $K(\mathbf{x}, \mathbf{y}) = (\text{scale} \cdot (\mathbf{x}, \mathbf{y}) + \text{offset})^{\text{degree}}$;
- the hyperbolic tangent kernel `tanhdot` given by $K(\mathbf{x}, \mathbf{y}) = (\text{scale}(\mathbf{x}, \mathbf{y}) + \text{offset})$,

and others.

```
> letter_prediction <- predict(letter_classifier, letters_test)
> head(letter_prediction)
[1] U N V X N H
Levels: A B C D E F G H I J K L M N O P Q R S T U V W X Y Z
> table(letter_prediction, letters_test$lettr)
letter_prediction A B C D E F G
A 144 0 0 0 0 0 0
B 0 121 0 5 2 0 1
C 0 0 120 0 4 0 10
D 2 2 0 156 0 1 3
E 0 0 5 0 127 3 1
F 0 0 0 0 0 138 2
G 1 1 2 1 9 2 123
(in abbreviated form)
```

```
> agreement <- letter_prediction == letters_test$letter
> table(agreement)
agreement
FALSE TRUE
643 3357
>
```