Suppose you are given a relation $R$ with four attributes $A B C D$ and the following set of FDs:
a. Identify the candidate key(s) for $R$
$F=\{A \rightarrow B, B \rightarrow C, D->B\}$.
$\mathrm{K}=$ ?
$\mathrm{F}+=$ ?
b. Is $R$ in $B C N F$ ? Is $R$ in 3NF? If it is not in BCNF, decompose to $B C N F$.

| $\mathbf{X}$ |  |
| :--- | :--- |
| A | A,B,C |
| B | B, C |
| C | C |
| D | D,B,C |
| AB | A,B,C |
| AC | A,C,B |
| AD | A,D,B,C |
| BC | B,C |
| BD | B,D,C |
| CD | C,D,B |
| ABC | A,B,C |
| ABD |  |
| ACD |  |
| BCD | $B, C, D$ |

$K=A D$
$F+=\{A \rightarrow B, B \rightarrow C, D->B, A->C, D->C\}$
BCNF?
BCNF Violation?
3NF Violation?

| A->B | YES | YES |
| :--- | :--- | :--- |
| B->C | YES | YES |
| D->B | YES | YES |
| A $>$ C | YES | YES |
| D->C | YES | YES |

NOT BCNF and NOT 3NF

If not BCNF, decompose.

Case 1:

$F x=\{A->B\}$
Attribute Closures for ACD

$\begin{array}{lll}D & D, C & F=\{A->C\} \\ A C & A, C & \\ A D & A, D, C & \\ C D & C, D & \end{array}$
Case 2:


