

a.

$$\pi_{\text{zipcode}} \left( \pi_{\text{sid}} \left( \pi_{\text{pid}} \left( \sigma_{\text{year}=2010} (\text{Parts}) \right) \bowtie \text{Orders} \right) \bowtie \text{Suppliers} \right)$$

b.

$$\pi_{\text{price}} \left( \pi_{\text{pid}} \left( \pi_{\text{sid}} \left( \sigma_{\text{state}='California'} (\text{Suppliers}) \right) \bowtie \sigma_{\text{quantity} \geq 10} (\text{Orders}) \right) \bowtie \text{Parts} \right)$$

c.

$$\pi_{\text{sname}} \left( \left( \pi_{\text{sid}} (\text{Orders}) - \pi_{\text{sid}} \left( \sigma_{\text{price} \leq 100} (\text{Parts}) \bowtie \text{Orders} \right) \right) \bowtie \text{Suppliers} \right)$$

d.

$$\pi_{\text{price}} \left( \pi_{\text{pid}} \left( \pi_{\text{sid}} \left( \sigma_{\text{zipcode}=102125} (\text{Suppliers}) \right) \bowtie \text{Orders} \right) \bowtie \sigma_{\text{price} > 200} (\text{Parts}) \right)$$

e.

$$\begin{aligned} & \rho(P_{2020}, \pi_{\text{pid}} \left( \sigma_{\text{year}=2020} (\text{Parts}) \right)) \\ & \rho(\text{Ordered}, \pi_{\text{pid}} (\text{Orders})) \\ & \rho(\text{Maine}, \pi_{\text{pid}} \left( \pi_{\text{sid}} \left( \sigma_{\text{state}='Maine'} (\text{Suppliers}) \right) \bowtie \text{Orders} \right)) \\ & \rho(\text{Valid}, (P_{2020} \bowtie \text{Ordered}) - \text{Maine}) \\ & \pi_{\text{pname}} (\text{Valid} \bowtie \text{Parts}) \end{aligned}$$

f.

$$\begin{aligned} & \rho(\text{High}, \pi_{\text{sid}} \left( \sigma_{\text{price}=1000} (\text{Parts}) \bowtie \text{Orders} \right)) \\ & \rho(\text{Low}, \pi_{\text{sid}} \left( \sigma_{\text{price} < 10} (\text{Parts}) \bowtie \text{Orders} \right)) \\ & \pi_{\text{zipcode}} \left( (\text{High} - \text{Low}) \bowtie \text{Suppliers} \right) \end{aligned}$$

g.

$$\begin{aligned} & \rho(O1, \text{Orders}) \\ & \rho(O2, \text{Orders}) \\ & \rho(\text{Two}, \pi_{O1.sid} \left( \sigma_{O1.sid=O2.sid \wedge O1.pid \neq O2.pid} (O1 \times O2) \right)) \\ & \pi_{\text{sname}} (\text{Two} \bowtie \text{Suppliers}) \end{aligned}$$

h.

$$\begin{aligned} & \rho(P1, \text{Parts}) \\ & \rho(P2, \text{Parts}) \\ & \rho(\text{Max}, \pi_{\text{pid}} (\text{Parts}) - \pi_{P1.pid} \left( \sigma_{P1.price < P2.price} (P1 \times P2) \right)) \\ & \pi_{\text{pname}} (\text{Max} \bowtie \text{Parts}) \end{aligned}$$

i.

$$\begin{aligned} & \rho(P1, Parts) \\ & \rho(P2, Parts) \\ & \rho(Max, \pi_{pid}(Parts) - \pi_{P1.pid}(\sigma_{P1.price < P2.price}(P1 \times P2))) \\ & \rho(Remaining, Parts - (Max \bowtie Parts)) \\ & \rho(R1, Remaining) \\ & \rho(R2, Remaining) \\ & \rho(Second, \pi_{pid}(Remaining) - \pi_{R1.pid}(\sigma_{R1.price < R2.price}(R1 \times R2))) \\ & \pi_{sid}(Second \bowtie Orders) \end{aligned}$$