Suppose you are given a relation R with four attributes $A B C D$ and the following set of FDs:
$F=\{B \rightarrow A, A C \rightarrow D\}$.
a. Identify the candidate key(s) for R
$\mathrm{K}=$ ?
$F+=$ ?
b. Is $R$ in $B C N F$ ? Is $R$ in 3NF? If it is not in BCNF, decompose to $B C N F$.

| $\mathbf{X}$ |  |
| :--- | :--- |
| A | A |
| B | B, A |
| C | C |
| D | D |
| AB | A,B |
| AC | A,C,D |
| AD | A,D |
| BC | B,C,A,D |
| BD | B,D,A |
| CD | C,D |
| ABC |  |
| ABD | A,B,D |
| ACD | A,C,D |
| BCD |  |

$K=B C$
$F+=\{B \rightarrow A, A C \rightarrow D, B C->D\}$

BCNF?

| BCNF Violation? |  | 3NF Violation? |
| :--- | :--- | :--- |
| B->A | YES | YES |
| AC->D | YES | YES |
| BC->D | NO (not BCNF violation) |  |

NOT BCNF and NOT 3NF

If not BCNF, decompose.

Case 1:


$$
F x=\{B \rightarrow A\}
$$

$$
F y+=\{B C->D\}
$$

Case 2:


