

Computational Models of Visual Tagging

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Abstract. The studies reported in this chapter exemplify the experimental-simulative approach of the interdisciplinary research initiative on “Situated Artificial Communicators”. Two experiments on visual tagging strategies are described. In Experiment 1, participants were presented with random distributions of identical dots. The task was to look exactly once at each dot, with a starting dot specified. This setting allowed a quantitative analysis of scan-path structures and hence made it possible to compare empirical scan paths to computer-generated ones. Five different scan-path models were implemented as computer simulations, and the similarity of their scan paths to the empirical ones was measured. Experiment 2 was identical to Experiment 1 with the exception that it used items of varying color and form attributes instead of identical dots. Here, the influence of the distribution of colors and forms on empirical scan paths was investigated. The most plausible scan-path models of Experiment 1 were adapted to the stimuli of Experiment 2. The results of both experiments indicate that a simple, scan path minimizing algorithm (“Traveling Salesman Strategy”; TSS) is most effective at reproducing human scan paths. We also found an influence of color information on empirical scan paths and successfully adapted the TSS-based model to this finding.

1. Introduction

One important aspect of situated communication is that it requires the interlocutors to generate comprehensive representations of their physical environment (Rickheit & Sichelschmidt, 1999). This is the case not only in task-oriented dialogue, where interlocutors, being part of the environment, collaborate in solving physical problems (e.g., Rickheit, 2005); this also applies to the production and comprehension of referential verbal expressions in general (e.g., Sichelschmidt, 2005). Locatives, for instance, can hardly be used without recourse to a visuo-spatial frame of reference (see Vorweg, Wachsmuth, and Socher, this volume). Successful reference to elements in the visual environment has as a prerequisite

a detailed exploration of the surrounding scene (Henderson & Ferreira, 2004). Visuolinguistic processing and scene exploration, in particular, the extraction of relevant information about what is located where in the scene, is mostly effortless. We are hardly aware of the fact that such scene perception is a serial process which involves adequate eye movements. The high efficiency of this process is not only based on the high speed of human eye movements, but also on our strategies to direct them (Findlay, 2004). These strategies have been optimized during a long period of evolution. They are crucial for our understanding of the human visual system, visuolinguistic information processing, and the construction of technical vision systems (Najemnik & Geisler, 2005). The studies reported here focus on a fundamental question: What factors determine the sequence in which we inspect a given set of items?

There are numerous approaches that have tried to provide at least partial answers to this question. Most experiments in the “classic” paradigm of visual search, but also in sophisticated variants such as comparative visual search, use simple, abstract stimuli. In classic visual search (e.g., Treisman & Sato, 1990; Wolfe, Cave & Franzel, 1989), participants are typically presented with a set of abstract items, such as letters or geometrical objects, and have to decide whether a designated target item is among them. In contrast, in comparative visual search (Pomplun, 1998; Pomplun, Sichelschmidt, Wagner, Clermont, Rickheit & Ritter, 2001), participants have to detect the only difference between two almost identical sets of objects. While most studies rely on reaction times and error rates as the principal indicators for search performance, several researchers have also investigated the visual scan paths taken during visual search or comparison (e.g. Koesling, 2003; Pomplun et al., 2001). Williams and Reingold (2001), for example, used a triple conjunction search task in which the presented items varied in the three dimensions color, form, and orientation. The authors analyzed the proportion of fixations on each distractor type. They found that the highest proportion of fixations was directed towards those distractors that were of the same color as the target. This finding suggests that it is possible to use color information for choosing an efficient scan path: Only the subset of items with the appropriate color has to be searched.

Eye-movement patterns during visual search or comparison and viewing images have been used as a basis for modeling visual scanning strategies (e.g.,

Koesling, Carbone & Ritter, 2003; Pomplun, Carbone, Sichelschmidt, Velichkovsky & Ritter, 2005). Several investigations were conducted by computer scientists intending to “teach” artificial vision systems to behave like the human visual system. Some models of human eye movements in realistic scenes use spatial filters in order to determine the most salient points in an image – the ones that are most likely to attract fixations (Parkhurst, Law & Niebur, 2002). These filters may be sensitive to contour features like sharp angles (Kattner, 1994) or to local symmetries (Heidemann, Nattkemper, Menkhaus & Ritter, 1996; Locher & Nodine, 1987). Rao and Ballard (1995) proposed a model of parallel search employing time-dependent filters. The location of the first fixation in a search process is determined by a coarse analysis (low spatial frequencies) of the given scene, and the following fixations are based on analyses of increasingly higher spatial frequencies. Another approach (Rimey & Brown, 1991) uses a Hidden Markov Model that is capable of learning efficient eye-movement behavior. It optimizes its scan paths iteratively towards highest efficiency of gathering information in a given scene. The Area Activation Model proposed by Pomplun, Reingold and Shen (2003) computes the informativeness and therefore the activation value of every point in the display, with more highly activated positions being more likely to be fixated than less activated positions. The scan path is determined by the method of local minimization of scan path length: The item fixated next corresponds to the activation peak closest to the current gaze position that has not been visited yet. Itti and Koch (2001) additionally emphasized the importance of the surrounding context for the saliency map and of top-down attentional processes. Recently, the saliency-based approach to visual attention has received some empirical support (Querhani, von Wartburg, Hügli & Müri, 2004).

To date, however, even the best attempts at computer vision are far from reaching the performance of the human visual system. One important reason for this fact might be that we do not completely understand the fundamental cognitive mechanisms which guide our attention so efficiently during the exploration of a scene. It seems that the scenes used in the modeling studies mentioned above are perceptually too complex to yield insight into these mechanisms. In real-world scenes, a viewer’s attention is guided by high-level factors, for instance, by the functional or conceptual relationships between items or the relevance of items to the viewer (Henderson & Hollingworth, 1999). It is almost

impossible to parameterize such high-level factors and to obtain quantitative, clearly interpretable results from this kind of experiments.

Another problem is that neither the search or comparison tasks nor the viewing tasks described above are particularly well-suited to investigate scene inspection strategies. Gaze trajectories in these tasks yield only relatively coarse information about the exact structure of scan paths, i.e. the sequence of items that receive attention. This is because visual attention can be shifted without employing eye movements. During rapid processes of scanning, minute “covert” shifts of attention are likely to occur (for discussions, see Posner, 1980; Salvucci, 2001; Wright & Ward, 1994). Therefore, gaze trajectories in search or viewing tasks do not indicate the whole sequence of attended items but – depending on task complexity and item density – only a small subset of it.

In order to obtain more comprehensive information about visual scan paths, we measured people’s eye movements in a simplified scanning scenario which we refer to as “visual tagging” (see Klein, 1988; Shore & Klein, 2000). In the visual tagging scenario, the participants viewed a random distribution of dots that were identical except that one of them – the starting dot – was conspicuously brighter than the others. The task was to look exactly once at each dot in the display, starting with the specified dot. This task is similar to the one used by Beckwith and Restle (1966), who asked people to count large sets of objects. By analyzing reaction times for different types of object configurations, Beckwith and Restle found that the participants grouped the objects into subsets in order to count them efficiently and to avoid mistakes. In our experiments, however, we eliminated any possible interference of a concurrent counting task with the scanning process. Furthermore, we used eye tracking to measure the exact temporal sequence of dots attended to.

On the one hand, the visual tagging task is rather artificial. In everyday life we are not used to strictly avoiding repeated attention to the same object, because the “cost” of a redundant eye movement is small (see Ballard, Hayhoe & Pelz, 1995). Although there is ample empirical evidence for an attentional mechanism called inhibition of return (Klein, 2000; Posner & Cohen, 1984; Tipper, Weaver, Jerreat & Burak, 1994), this mechanism alone is not sufficient to generate self-avoiding and complete scan paths as demanded by our task. Therefore, people’s scan paths are likely to be influenced by cognitive processes oper-

ating at a higher level than those being usually involved in natural situations, e.g., free exploration of surroundings. In particular, path planning processes are expected to take place, because people have to hold in memory which dots they have already visited during task completion (Beckwith & Restle, 1966; Melcher & Kowler, 2001).

On the other hand, our task enabled us to investigate scan paths purely based on the stimulus geometry, i.e. on the locations of the dots. Neither item features nor relations between them (other than geometrical relations) biased the observed strategies. Moreover, the demand of attending exactly once to each item brought about an enhanced comparability of scan paths taken on the same stimulus. Restricting the analysis to those paths that met this demand made it easy to define a measure of similarity: The degree of similarity of a path *A* to another path *B* was calculated as the number of “jumps” (edges) between dots that appear in path *A* as well as in path *B*.

Experiment 1 investigated geometrical regularities of scan paths with the aim of identifying possible mechanisms that control human tagging strategies in scene inspection. Several models of such mechanisms were developed and implemented as computer simulations. The simulated scan paths were then compared to the empirical ones in order to evaluate the plausibility of the proposed mechanisms. Another important question was whether there are preferred directions of scan paths. In other words, does the rotation of the stimuli exert an influence on the scan paths?

Experiment 2 went one step further towards a more naturalistic setting: While the participants’ task remained the same as in Experiment 1, the displayed items were given different color and form attributes. Beckwith and Restle (1966) showed that the distribution of color and form attributes influenced the time needed for counting a set of objects, with color having a substantially stronger effect than form. With the help of eye movement tracking, Experiment 2 directly investigated the influence of color and form on empirical scan paths. Moreover, the most successful models of Experiment 1 were refined in such a way as to account for this additional influence.

2. Experiment 1: Geometrical Factors

2.1. Method

Participants. Twelve students from different faculties of the University of Bielefeld took part in Experiment 1 in return for payment. All of them had normal or corrected-to-normal vision; none of them was color-blind or had pupil anomalies.

Apparatus. Stimuli were presented on a 17" ViewSonic 7 monitor. The participants' eye movements were measured with the OMNITRACK 1 system (see Stampe, 1993). The system uses two video cameras as inputs of information about the position of the head relative to the environment and the position of the pupil relative to the head. This technique allows the participants to move their head from the straight-ahead position up to 15° in all directions, and therefore provides natural viewing conditions. Gaze positions are recorded at a frequency of 60 Hz. Fixations are calculated using a speed threshold in a 5-cycle time window, which means that only fixations with a duration of at least 83 ms are detected. The absolute spatial precision of the gaze-position measurement ranges from 0.7° to 1° . By using a calibration interface based on artificial neural networks (Parametrized Self-Organizing Maps), we improved the system's precision to approximately 0.5° (see Pomplun, Velichkovsky & Ritter, 1994).

Stimuli. Participants were presented with displays showing 30 dots (diameter of 0.5°) randomly distributed within a square area (18° per side) on a black background. The dots were of the same color (blue), with a designated starting dot being clearly brighter than the others (for a stimulus sample, see Figure 1, left). Five different dot configurations were randomly generated. In order to investigate directional effects on the scan paths, for instance top-to-bottom or left-to-right strategies corresponding to the viewers' direction of reading, each configuration was shown in four different orientations (rotated by 0° , 90° , 180° , and 270°). This resulted in a set of 20 stimuli used in Experiment 1.

Procedure. A written instruction informed the participants about their task. They had to look at each dot in the display once, beginning with the starting dot. Participants were told not to miss any dots or to look at any of them more than once. Furthermore, participants had to attend to each dot for at least half a sec-

ond to make sure that they actually performed a saccade rather than a covert shift of attention towards the dot. After task completion the participants were to press a mouse button. The experiment started with two practice trials followed by the eye tracker calibration procedure and the 20 recording trials in random order. Each trial was preceded by a short calibration for drift correction, using a single target at the center of the screen.

2.2. Results

The recorded gaze trajectories were converted to item-based scan paths. In other words, the temporal order of attended dots had to be reconstructed, because our analysis was intended to refer to these rather than to fixation points. It turned out that this could not be done automatically. The occurrence of additional fixations (conceivably used by the participants to get their bearings), imprecise saccades as well as errors in measurement required human post-processing. Consequently, an assistant – who was naive as to the purpose of the study – did the allocation of fixations to dots manually, on the basis of the individual trajectories with sequentially numbered fixations superimposed on the stimuli. As a result of this semi-interpretative analysis, only 139 of the 240 converted paths (57.9%) were found to be consistent with the task, i.e., they visited each dot exactly once. The further analyses were restricted to these paths.

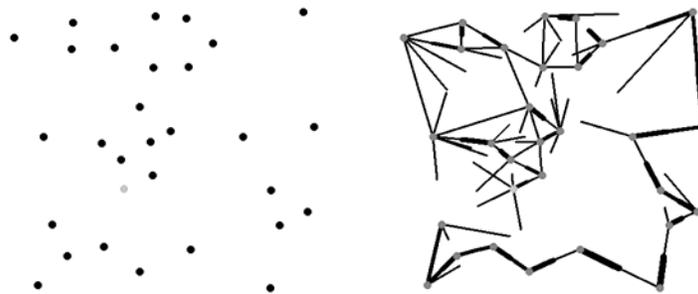


Figure 1. Sample stimulus (left) and corresponding visualized results (right).

Figure 1 presents a visualization of accumulated data (right panel) for a sample stimulus (left panel). Thicker lines between dots indicate transitions (edges) used by a larger number of participants. The lines are bisected due to the two possible directions to move along these edges. Each half refers to those transitions that started at the dot next to it. Halves representing fewer than three transitions are not displayed for the sake of clarity. Figure 1 illustrates that in the absence of any conspicuous order (as in the upper left part of the sample stimulus) there is high variability of chosen edges across participants, whereas the linearly arranged dots (such as those on the right and at the bottom of the sample stimulus) were almost always scanned in the same order.

In addition, the quantitative analysis of the data allowed us to investigate the effect of rotating the stimuli: Were there directional influences on the scan paths, for example according to the viewers' reading direction? This was analyzed by comparing similarities (as defined above) between the scan paths of different participants. If the scan paths for the same stimuli shown in the same orientation were more similar to each other than the ones for different orientations of the same stimuli, this would indicate that the rotation exerted an effect. In fact, the average similarity value for the same orientation was 19.43 edges per path, while the value between different orientations was 19.42, constituting no significant difference, $t < 1$. Consequently, it was justified not to assume any directional influence. So we averaged the data for each of the five original stimuli over its four different orientations for all subsequent analyses.

2.3. Modeling Tagging Strategies

We developed and evaluated five different models of tagging behavior. Since the empirical data showed no significant dependence on the orientation of the stimuli, none of the models developed below include this factor. In order to obtain baseline data for the evaluation of the models, we calculated a composite path with maximal similarity to the observed paths ("optimum fit") for each stimulus. An iterative algorithm determined this path within the huge set of all possible acceptable paths, regardless of whether the path actually appeared in any one participant's data. The average similarity of optimum fit paths to empirical paths turned out to be 21.89, which exceeded the similarity of empirical ones to each

other (19.43, cf. above). The calculation of optimum fit paths also shows that no simulation can produce paths of higher similarity to the empirical data than 21.89, which is considerably lower than the perfect similarity (identity) value 29 (all acceptable paths consist of 29 edges). This discrepancy demonstrates the high intrinsic variability of scan paths.

Serving as a second baseline, the similarity of completely randomly generated scan paths to the empirical paths was computed, yielding a value of as low as 1.75. A sample optimum fit path as well as sample paths computed by the models are given in Figure 2, referring to the sample stimulus in Figure 1. The five models that were evaluated are described below.

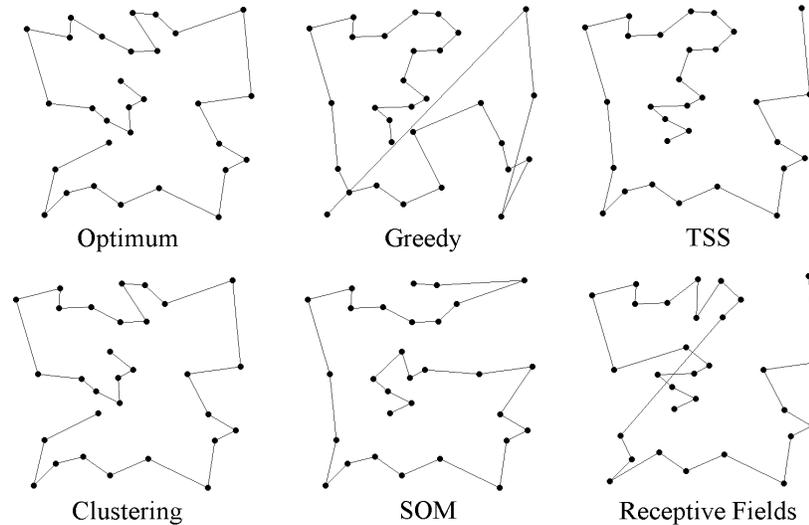


Figure 2. Scan paths generated by the different models, plus the optimum fit path, for the sample stimulus shown in Figure 1.

The “Greedy” Heuristic. One model that suggests itself for analysis is based on what can be termed the “Greedy” heuristic. Among all dots that still need to be visited, the Greedy algorithm always jumps to the one that is geometrically nearest to the current “gaze” position. Although it produces plausible, locally

optimized sections of scan paths, the Greedy strategy has one drawback: On its way through the stimulus, it leaves aside items of high eccentricity. As a consequence, these items have to be “collected” later, which leads to unnaturally long saccades at the end of the scan path. The lack of memory constitutes a fundamental difference from empirically observed strategies. Nevertheless, even this simple model achieves a similarity value of 17.36, indicating that its strategy of always choosing the nearest item, that is, the local minimization of scan paths, is already tremendously better than a purely random strategy.

The “Traveling Salesman” Algorithm. The shortcoming of the Greedy heuristic motivates the implementation of a “Traveling Salesman Strategy” (TSS) algorithm. The Traveling Salesman Problem is a basic paradigm in computer science: A salesman who has to successively visit a certain number of places wants to save time and energy, so his problem is to find the shortest path connecting all the places. In the present context, this means that the TSS Model algorithmically minimizes the overall length of its scan paths rather than just the length of the next jump. However, unlike standard TSS, the paths of this algorithm do not return to the starting dot. In the current formulation, only the choice of the first dot is constrained. The results show that this simulation gets much closer to the actual human strategies than the Greedy heuristic: The similarity value is 20.87, which is fairly close to the optimum fit value of 21.89. This finding suggests that not only the local optimization of scan paths – as operationalized in the Greedy algorithm – plays an important role in human scan path selection, but also their global optimization.

The Clustering Model. The fact that the TSS Model has yielded the best result so far motivates the investigation of a refined variant of it. Consequently, we built a “Clustering Model” that is based on the assumption that human scan paths are generated by clusterwise processing of items (cf. Beckwith & Restle, 1966). The model divides the process of scan-path computation into two steps. In the first step, the configuration of items is divided into clusters. A clustering algorithm maximizes the between-cluster distances and minimizes the within-cluster distances with the help of a cost function. We set the parameters of this iterative procedure in such a way that it generates clusters that may have either compact or linear shape. Five to seven clusters with four to seven items each are calculated, which is perceptually plausible (see Atkinson, Campbell & Francis,

1976; Miller, 1956). The second step consists in a TSS algorithm calculating local scan paths of minimal length connecting the dots within each cluster, as well as a global scan path of minimal length connecting all clusters. Afterwards, the within-cluster scan paths are linked together in the sequence specified by the between-cluster scan path. Thus, this model processes all dots within a cluster before proceeding to the next one, thereby operating like a hierarchical TSS algorithm. A similarity analysis showed that the Clustering Model selects paths slightly more similar to the empirically observed ones (21.12) than does the TSS Model. This may suggest that clustering is a component of human scanning strategies.

The Self-Organizing Map Approach. When simulating cognitive processes we should also consider neural network approaches, as their functional structure is biologically motivated. An appropriate neural paradigm is provided by Kohonen's self-organizing maps (SOMs), which are capable of projecting a high-dimensional data space onto a lower-dimensional one (see Kohonen, 1990; Ritter, Martinetz & Schulten, 1992). SOMs are networks of simulated neurons, usually a one-dimensional chain or a two-dimensional layer. They learn in an unsupervised way to partition a given feature or input space into disjoint classes or areas and to represent their class by a typical feature vector. The feature space is a region of a classical vector space, where each vector $(v_1, v_2, \dots, v_n)^T$ shows n different features or input signals. These vectors are presented to the network in random order, and a neuron fires if its stored feature, that is, its position vector, is the best approximation to the active input position to the network. Thus we create a map – the neural network – in which each mapped point – each neuron – represents a region of input patterns. If we also ensure that the topology of the input space is preserved, i.e., that neighboring feature vectors are mapped to neighboring neurons, or neighboring neurons stand for similar features, we get a low-dimensional structure representing a possibly high-dimensional input. This is done by iterating the following steps:

- Choose a random input vector \mathbf{v} from feature space.
- Select a neuron j with $|\mathbf{v} - \mathbf{w}_j| \leq |\mathbf{v} - \mathbf{w}_i|, \forall i \neq j$, i.e., the neuron with the best representation \mathbf{w}_j of \mathbf{v} ; this is called the winner.
- Change all neuron weights \mathbf{w}_i towards the input vector \mathbf{v} , with an adaptive step size h_{ij} that is a decay function of the network distance between neuron i and the winner j . Here, ε is an additional global adaptive step size parameter:

$$\mathbf{w}_i^{\text{new}} = \mathbf{w}_i^{\text{old}} + \varepsilon \cdot h_{ij} \cdot (\mathbf{v} - \mathbf{w}_j), \varepsilon \in [0, 1].$$

The change of neuron weights adjusts $\mathbf{w}_i^{\text{old}}$ towards a better representation vector and the smooth distribution of change around the winner produces the desired topology preservation. In our case, we are only interested in a mapping from discrete 2D points onto a linear chain representing fixation order. Hence, the feature space is only the discrete set of dot positions in \mathbf{R}^2 , one of them labeled as starting dot. Since the chain must begin at the starting dot, the first neuron is defined to be the winner if the starting dot is presented, irrespective of the actual feature-vector difference. In order to make sure that all dots are represented by neurons after the learning process, the network contains a number of additional nodes. Now, the probability to skip a dot is very low, but more than one neuron may become mapped to the same position. This must be resolved by a post-processing step to extract the simulated scan path from the chain of neurons. The paths generated by this model look quite natural at first sight. Their similarity to the human ones, however, is substantially lower (19.45) than the results obtained by the TSS-based models.

The Receptive Field Simulation. Another biologically motivated approach in our set of models uses neurons with a particular type of receptive fields. In a neural network, natural or artificial, the term receptive field stands for the region of input space that affects a particular neuron (see, e.g., Hubel & Wiesel, 1962; Lennie, Trevarthen, van Essen & Wässle, 1990). Furthermore, the influence of stimuli in this region is not necessarily homogeneous, but dependent on variables such as the distance of the input vector from the center of the region. There may also be excitatory and inhibitory subregions, where a stimulus will respectively increase or decrease the activation of the neuron.

In our model, the receptive fields consist of an inhibitory axis and two laterally located, excitatory areas of circular shape (see Figure 3). We use 100,000 receptive fields that are randomly distributed across the input space. Their sizes vary randomly between 80% and 120% of the size of the relevant input space, i.e. the whole area in which dots are presented. There are eight possible orientations which are randomly assigned to the receptive fields. It is obvious from this description that the receptive fields are closely packed and overlap each other.

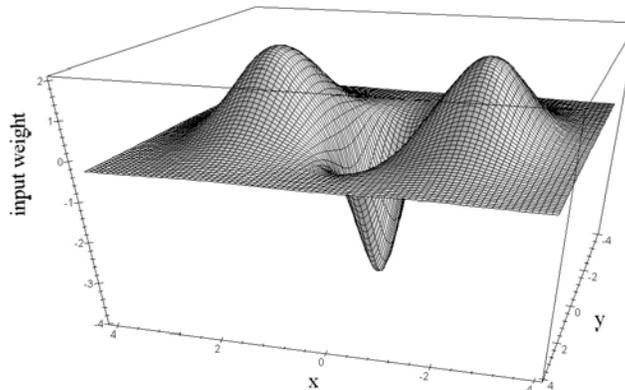


Figure 3. Illustration of the simulated receptive fields. The planar input space is represented by the dimensions x and y . Positive values of input weight signify excitatory connections, negative values signify inhibitory connections.

The activation of a neuron is highest if no dot is in the inhibitory region of the neuron's receptive field and as many dots as possible are in the lateral excitatory regions. The neuron with the highest activation (the winner neuron) thus indicates the most pronounced linear gap between two laterally located accumulations of dots. Therefore, the inhibitory axis of this neuron's receptive field can be considered to indicate the perceptually most plausible bisection of the stimulus.

This first bisection separates the set of dots into two subsets. Each subset serves as the input to a new group of neurons with smaller receptive fields, calculating further bisections. This procedure is repeated until none of the sections contains more than four dots, since the number four is a plausible minimum estimate of the number of dots that can be perceived at the same time (see Atkinson, Campbell & Francis, 1976; Miller, 1956). In Figure 4 (left), the model's hierarchical partitioning of the sample stimulus previously shown in Figures 1 and 2 is presented. The bisections are visualized by straight lines with numbers indicating their level in the hierarchy. The calculation of this structure – a binary tree – is our attempt to simulate a viewer's perceptual processing of the visual scene.

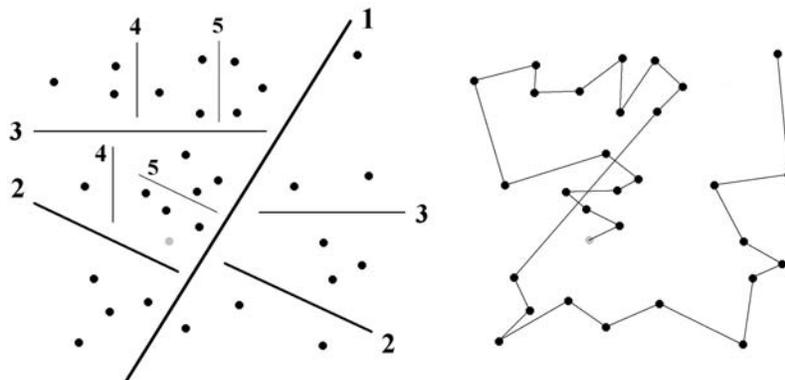


Figure 4. The model's hierarchical bisections (left) and the resulting scan path (right) for the sample stimulus shown in Figure 1.

Finally, the scan path is derived by a TSS algorithm calculating the shortest scan path that begins at the starting dot. In the present context, however, it is not the geometrical distance that is minimized, but a linear combination of the geometrical distance and the tree distance between the dots. The tree distance between two dots A and B is the minimum number of edges in a path connecting the subsets A and B in the tree structure. If we choose the coefficients of the linear combination in such a way that the tree distance is more relevant than the geometrical distance, the model generates the scan path shown in Figure 4 (right panel). It strictly follows the hierarchical tree structure, which leads to geometrical deviations.

As long as the model's linear coefficients are chosen such that the tree distance exerts a significant effect, neither the appearance of the simulated scan paths nor their calculated similarity to the empirical paths is convincing. When balancing the weights of the tree distances and the geometrical distances, we obtained scan paths with a similarity to the human paths of 18.73. The receptive field approach, at least in this rather simple form, does not seem to yield more plausible scan paths than does the TSS Model. This suggests that hierarchical partitioning does not seem to be an important perceptual mechanism underlying human visual tagging behavior.

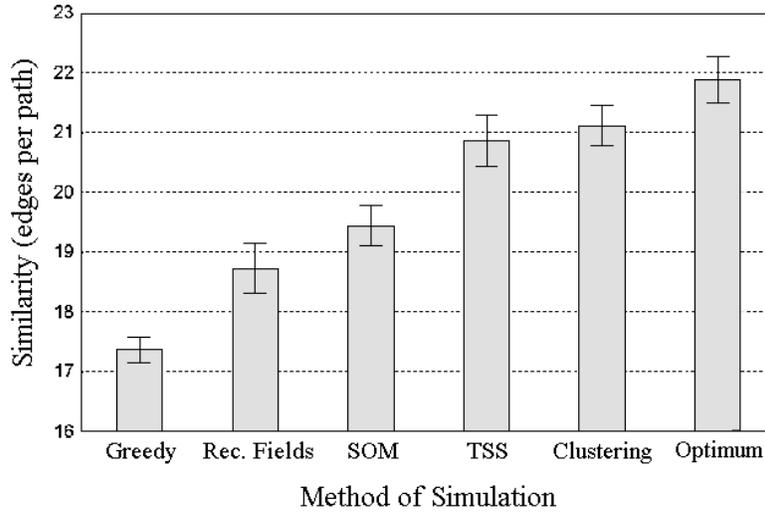


Figure 5. Similarity between the paths generated by the different models and the empirical scan paths, shown in ascending order, plus the optimum fit value

Model Comparison. Figure 5 displays a summary of the accuracies with which the various models simulate human scanning patterns, and it compares them to the optimum fit value. A one-way analysis of variance (ANOVA) was conducted on these data, excluding the optimum fit value, which was a global value that did not vary across individuals. The ANOVA revealed a significant main effect showing differences between the similarity values, $F(4;44) = 32.34$, $p < 0.001$. Pairwise t -tests with Bonferroni-adjusted probability values were conducted to examine these differences more closely. All of the models reached significantly higher similarity than the Greedy heuristic, all $t(11) > 3.62$, $p < 0.005$. The Receptive Fields Model did not significantly differ in results from the SOM Model. These two models, in turn, were outperformed by both the TSS Model and the Clustering Model, all $t(11) > 4.84$, $p < 0.01$. Finally, the TSS Model did not significantly differ from the Clustering Model, $t(11) < 1$.

2.4. Discussion

Basically, the results of Experiment 1 show that the simple TSS Model and Clustering Model yield better scan paths than the neural models, and that even the simple Greedy algorithm is not far behind. This finding should not be interpreted as evidence for a general incapability of neural models to explain scan-path mechanisms. The neural models tested in Experiment 1 were of a very primitive nature. Multi-layered networks might be able to generate scan paths more similar to the empirically observed ones. Moreover, discretion is advisable in the interpretation of these data, since they are based on only five different dot configurations. Nevertheless, from the results above we can conclude that it is difficult to generate better simulations of human scan paths than those created by the simple TSS-based models. Thus the minimization of scan-path length seems to be a basic principle in human scanning strategies.

Another important result of Experiment 1 is the independence of scan paths from rotations of the stimuli. In other words, the order in which a viewer scans a set of dots does not seem to change when the display is rotated by 90, 180, or 270 degrees. It is well-known from visual search experiments (e.g. Zelinsky, 1996; Pomplun, 1998) that viewers prefer to scan a display according to their reading direction, if they are allowed to freely choose the starting point. However, this was not observed in the present study. A possible reason is that the specified starting point induced rotation-invariant scanning strategies.

3. Experiment 2: Color and Form Attributes

The objective of Experiment 2 was to investigate the influence of color and form attributes on scan paths. Participants were presented with distributions of geometrical objects (squares, triangles, and circles) in different colors (yellow, blue, and green). We might expect color and form to influence the structure of chosen scan paths, because viewers are likely to take advantage of the additional structural information. As their main concern is to remember which of the items they have already visited, the introduction of color and form features might allow them to use perceptual groups of identical attributes as scan-path units which

need less effort to remember than do single items. This assumption is supported by the results of Beckwith & Restle's (1966) counting task. They found shorter reaction times when object colors were clustered, i.e. different colors were spatially segregated. They also found an analogous – but weaker – effect for clustering the objects by form. To examine potential corresponding effects on scan-path structure, the stimuli in Experiment 2 had three different levels of color and form clustering.

If humans make use of the color or form information, these effects should be integrated into the models. It is plausible to assume that the attributes lead to a reduction in scan-path variability, which could enable the models to yield better results than in Experiment 1. Here we took advantage of the findings of Experiment 1: Since the paths generated by the TSS and Clustering Models were most similar to the empirical data, we focused on the adaptation of these two approaches to the stimuli used in Experiment 2. In order to make the two experiments easier to compare, the design and procedure of Experiment 2 corresponded to Experiment 1. Based on the results of Experiment 1, however, we did not further investigate the effect of stimulus rotation. In addition, the introduction of color and form attributes required to change the way of indicating the starting item. In Experiment 2, we used a dynamic cue, namely a flashing red circle around the starting item, appearing for a short period after stimulus onset. This method of marking the starting item did not alter its color or form attributes. The participants' task was the same as in Experiment 1, namely to look once, and only once, at each item.

3.1. Method

Participants. Twenty new participants from different faculties of the University of Bielefeld took part in Experiment 2 in return for payment. They had normal or corrected-to-normal vision; none was color-blind or had pupil anomalies.

Apparatus. The apparatus was the same as in Experiment 1.

Stimuli. The stimuli consisted of 30 simple geometrical items (diameter of about 0.7°) of three different colors (fully saturated blue, green, and yellow) and three different forms (triangle, square, and circle) on a black background. Their spatial distribution was randomly generated within a display of 18° by 18° with a minimum distance of 1.5° between the centers of neighboring items in order to

avoid item overlap or contiguity (see Figure 6). In each stimulus array, there were a balanced number of items with each color and form. The distribution of colors and forms was not always homogeneously random, as they were clustered to varying degrees in most trials. To explain the clustering algorithm, a formalized description of the stimulus patterns is necessary: A pattern is a set of N items (objects)

$$\mathbf{o}^{(n)} = \begin{pmatrix} o_x^{(n)} \\ o_y^{(n)} \\ o_c^{(n)} \\ o_f^{(n)} \end{pmatrix}, \quad n = 1, \dots, N,$$

where $(o_x^{(n)}, o_y^{(n)})$ is the pixel position of the item's center in the display, $o_c^{(n)}$ is the item's color (1 = blue, 2 = green, 3 = yellow), and $o_f^{(n)}$ is the item's form (1 = square, 2 = triangle, 3 = circle).

Now the variable color clustering α_c is introduced. It is defined as the ratio between the mean distance $d_{c,dif}$ between all pairs of items with different colors and the mean distance $d_{c,id}$ between those with identical colors:

$$\alpha_c = \frac{d_{c,dif}}{d_{c,id}}$$

$$d_{c,dif} = \frac{\sum_{n_1=1}^N \sum_{n_2=n_1+1}^N \mathbb{1}_{o_c^{(n_1)} \neq o_c^{(n_2)}} \Delta(n_1, n_2)}{\sum_{n_1=1}^N \sum_{n_2=n_1+1}^N \mathbb{1}}$$

$$\Delta(n_1, n_2) = \sqrt{(o_x^{(n_1)} - o_x^{(n_2)})^2 + (o_y^{(n_1)} - o_y^{(n_2)})^2}$$

For example, a value $\alpha_c = 2$ would mean that, on average, items of different colors are twice as distant from each other than items of the same color. In our setting of 30 items and three different colors this would correspond to a strongly

segregated distribution containing large single-colored areas. $\alpha_c = 1$ would mean that there is no clustering at all. We define the parameter form clustering α_f analogously.

Figure 6 illustrates the correspondence between α_c , α_f , and the distribution of colors and forms in four different sample stimuli. While the panels (a) to (c) display stimuli with increasing color clustering and no form clustering, panel (d) shows a stimulus with high color and high form clustering. These examples demonstrate an important feature of α_c and α_f for the present experiment: Color and form clustering can be varied independently from each other. Even in an array with both high color and form clustering, the separate concentrations of colors and forms usually do not correspond.

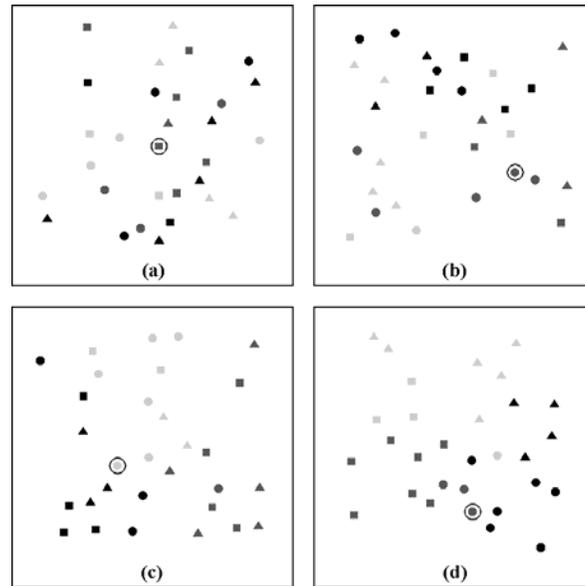


Figure 6. Examples of item distributions with different levels of color/form clustering: (a) no color and form clustering (1.0/1.0), (b) weak color and no form clustering (1.3/1.0), (c) strong color and no form clustering (1.7/1.0), and (d) strong color and form clustering (1.7/1.7). Circles indicate the starting items.

An iterative algorithm for generating color and form distributions with given parameters of color clustering α_c and form clustering α_f can easily be implemented. Starting with a random distribution, this algorithm randomly selects pairs of items and exchanges their color or form attributes, if this exchange shifts the distribution's clustering levels towards the given parameters. The algorithm terminates as soon as the difference between the actual and the desired α_c and α_f falls below a certain threshold, which was set to 0.05 in the present study.

Three different levels of color and form clustering were used, namely “no clustering” (1.0), “weak clustering” (1.3), and “strong clustering” (1.7). Examples of stimuli at these levels can be seen in Figure 6. The nine possible combinations of different levels of color and form clustering constituted the stimulus categories of Experiment 2. Five stimuli of each category were used, leading to a total of 45 different stimuli. For two seconds after stimulus onset, a flashing red circle was shown around one of the items, signifying the starting item which was always the same across individuals for each given stimulus.

Procedure. The procedure was the same as in Experiment 1, except that 45 trials were conducted in random order.

3.2. Results

As in Experiment 1, an assistant converted the recorded fixations into scan paths connecting the items in the display. The assistant was only shown the locations of the items, but not their color or form attributes. Just like in Experiment 1, the superimposed visualization of the participant's fixations and their temporal order allowed the assistant to mark the individual scan path item by item. The proportion of acceptable paths was 93.3%, which was substantially higher than in Experiment 1 (57.9%). Apparently, the additional color and form information helped the participants not to “get lost” during task completion. The individual features of the items seemed to facilitate reliable memorization and recognition. The incorrect paths were approximately equally distributed among the nine categories of stimuli, and so were excluded from the analysis.

For a qualitative analysis, we can inspect the calculated scan paths of maximal similarity to the empirical ones (optimum fit). The upper row of Figure 7 presents these paths for an unclustered, a strongly color-clustered, and a strongly

form-clustered stimulus. There is no obvious evidence for the influence of color or form attributes on the viewers' strategy. Although there are some longer sections of scan paths exclusively visiting items of the same color or form, these items are always located closely together. This qualitative finding suggests that the location of items remains the most important factor to determine the structure of scan paths.

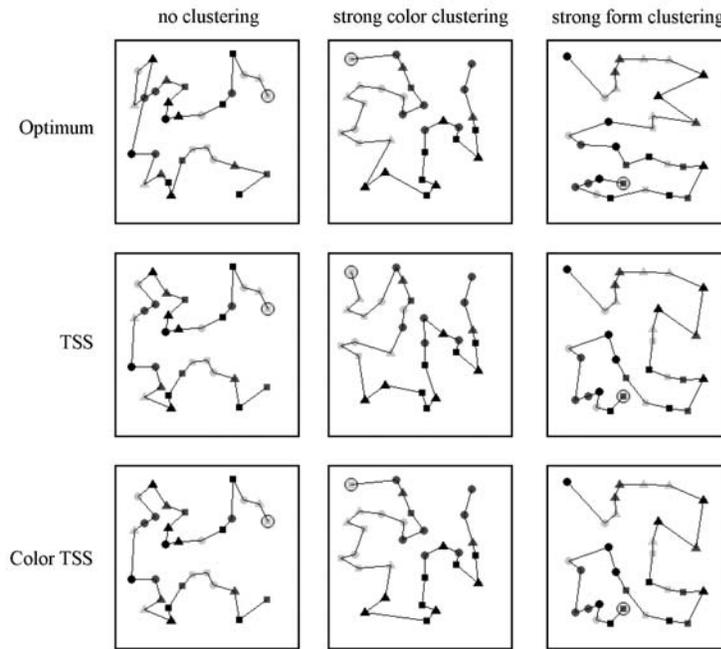


Figure 7. Scan paths generated by participants (optimum fit paths), the TSS Model, and the Color TSS Model. Circles indicate the starting items.

The quantitative investigation of the effects of color and form required a measure of color and form clustering within the empirically observed scan paths. An appropriate choice seemed to be the mean runlength with regard to these dimensions. In the present context, a run is defined as a sequence of items of the same color or form within a scan path. The runlengths ranged from one to ten, as there

were always exactly ten items of each color and form in each stimulus array. In order to calculate a mean runlength across multiple paths, we employed a weighted mean to equally account for every single transition between items. Since longer runs comprise more transitions, we weighted each run with its runlength.

However, it is important to verify whether this measure indeed reflects the influence of item attributes rather than the geometrical structure of the stimulus. Even a participant who completely ignores color and form would generate longer runs with increasing strength of clustering in the stimulus. This is due to the fact that, according to the results of Experiment 1, viewers seem to prefer short scan paths, so neighboring items are disproportionately likely to be scanned successively. Clustering moves items with the same features closer together and thus increases the average color and form runlengths in empirical scan paths.

Fortunately, there is a “color and form blind” model, which yields paths of high similarity to the empirical ones, namely the TSS Model. We applied the TSS Model to each stimulus used in Experiment 2 to generate baseline predictions about the color and form runlengths in that stimulus. In a comparative analysis of observed scan paths, we then divided all color and form runlengths by the TSS-predicted runlengths, thereby obtaining relative runlengths. Rather than absolute runlengths, relative runlengths reveal the influence of item attributes on an individual’s scan path. Relative color runlength 1, for instance, would indicate no difference to the TSS Model and thus no influence of color attributes on empirical scan paths. Longer relative runlengths would indicate increasing influence.

Figure 8 shows the participants’ relative color and form runlengths at the three levels of color and form clustering respectively. A two-way ANOVA revealed significant main effects of the two factors dimension (color vs. form), $F(1; 19) = 9.97, p < 0.01$, and strength of clustering (no vs. weak vs. strong clustering), $F(2; 38) = 4.77, p < 0.05$. There was also a significant interaction between the two factors, $F(2; 38) = 5.81, p < 0.01$, which was due to the fact that clustering had a significant effect on relative color runlength, $F(2; 38) = 5.56, p < 0.01$, but not on relative form runlength, $F(2; 38) = 2.36, p > 0.1$. For the color dimension, pairwise t -tests with Bonferroni-adjusted probabilities revealed

a significant difference between no clustering (1.092) and strong clustering (1.213), $t(19) = 3.94$, $p < 0.005$. The differences to the weak clustering condition (1.131), however, were not significant, both $t(19) < 1.67$, $p > 0.3$. Finally, the overall relative color runlength (1.145) differed reliably from the value 1, $t(19) = 3.41$, $p < 0.005$, whereas overall relative form runlength (0.999) did not, $t < 1$.

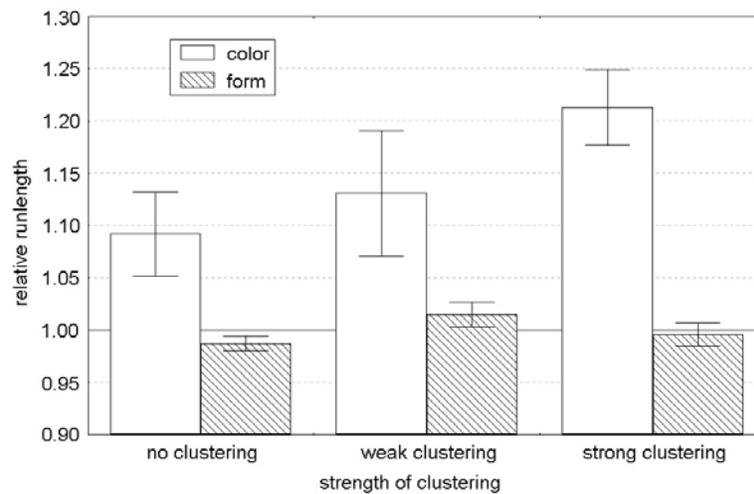


Figure 8. Mean relative color and form runlengths as functions of the strength of color and form clustering respectively.

Taken together, these findings suggest that viewers use color information to guide their scan paths, because the color runlength in their scan paths is longer than predicted by the TSS Model. This effect of color guidance increases with the strength of color clustering in the stimuli. The participants' form runlengths, however, do not exceed the predicted ones and do not depend on form clustering in the stimuli. Hence, we assume that viewers do not use form information when performing the task.

3.3. Refinement of Scan Path Models

The results of Experiment 1 motivated the adaptation of both the TSS Model and the Clustering Model to stimuli containing items with color and form attributes. Since the Clustering Model can be viewed as a refinement of the TSS Model, we started with adjusting the TSS Model. The first question was how we could bias the TSS algorithm to react to color in the same way as the average viewer does. Basically, the model should still calculate scan paths of minimal length, but in doing so, it should weight the purely geometrical distances by the color (in)congruence (color distance) between the neighboring items. Such a weighting is achieved by multiplying the distance between two items of different colors by a constant factor – the color weight – and leaving the distance between items of the same color identical to their geometrical distance.

Obviously, the algorithm's behavior will then strongly depend on the color weight. A color weight of 1 would lead to a standard TSS algorithm, which would not be influenced by color information at all. In contrast, a color weight of, say, 1000 would make the algorithm use a minimum of transitions between different colors. Regardless of the arrangement of items, the algorithm would first visit all items of the starting item's color *A*, then inspect all items of color *B*, and finally those of color *C*. Within the color groups it would behave like a conventional traveling salesman algorithm, taking the shortest passages possible. By adjusting the color weight it is possible to control the influence of colors and hence the average color runlength produced by the TSS algorithm. Since the goal is to adapt the TSS Model to the empirical data, i.e. to produce the same runlengths as generated by the participants, the color weight needs to be adjusted for the best match.

What is the response of the TSS algorithm to increasing the color weight? As might be expected, it reveals a tendency towards the avoidance of transitions between items of different colors, because these transitions increase the overall length of the scan path above proportion. Figure 9 shows color runlength as a function of the color weight ranging from 1.0 to 1.5. The mean runlengths are displayed separately for each of the three levels of color clustering in the stimuli. Additionally, the empirically obtained runlengths for these levels are shown as horizontal lines.

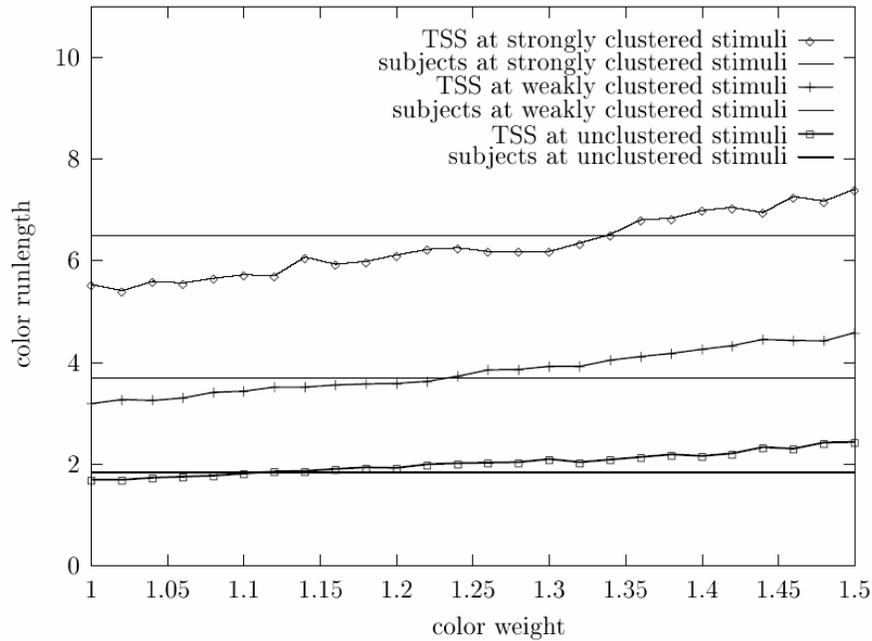


Figure 9. Color runlength generated by the TSS Model as a function of the strength of color clustering and the introduced color weight. Horizontal lines indicate empirical runlengths.

We find the TSS runlengths to increase approximately linearly with increasing color weight. Higher levels of clustering lead to steeper runlength slopes. Interestingly, there is no single value of the color weight to yield the best-matching runlengths for all levels of clustering. For each level, the intersection between the runlength curve of the TSS Model and the participants' runlength occurs at a different color weight. These are the values 1.11 for the no clustering condition, 1.23 for weak clustering, and 1.33 for strong clustering. Loosely speaking, the viewers seem to apply higher color weights with increasing color clustering in the display.

In light of these data, we must consider if the introduction of color weights, as described above, is an adequate method of modeling the observed color effects. Since the model needs different color weights depending on the strength of color clustering, we have to pose the question whether this approach is really plausible. An alternative idea would be to assign color weights for sequences of transitions rather than for single transitions. Starting with the value 1.0, the color weight for a whole group of successive transitions within the same color would decrease linearly with the number of items in that group. This arrangement would make the choice of longer color runs increasingly attractive to the TSS algorithm. However, testing this approach yielded a result that was in some respects inverse to the previous one: For increasing levels of color clustering, the alternative method needed decreasing weights for long color runs in order to produce scan paths of good similarity to the empirical ones.

To solve this problem, we could try to combine the two approaches or to use more complex functions to determine the relevant distances between items. A basic rule of modeling is, however, to use as few freely adjustable parameters as possible. The more of these parameters are integrated into a model, the easier it is for the model to fit any data, which weakens the reliability of conclusions drawn from the model's performance. Therefore, we kept our desired model, which we named the Color TSS Model, as simple as possible by extending our initial approach. Figure 9 suggests a linear dependence of the required color weight on the strength of color clustering. Recall that the three levels of color clustering correspond respectively to the values 1.0, 1.3, and 1.7 on the cluster measure α_c , with a maximum deviation of 0.05. We determined the parameters of the linear function to yield runlengths most similar to the empirical ones:

$$\text{color weight} = 0.264 \alpha_c + 0.799$$

Three sample paths generated by the resulting Color TSS Model are shown in the lower row of Figure 7. In fact, some subtle differences to the TSS paths (middle row) can be found indicating that the new model better corresponds to the empirically observed strategies (upper row). A similarity analysis showed that the scan paths generated by the Color TSS Model were indeed more similar

to the observed patterns (similarity value 19.51) than those produced by the unadjusted TSS Model (19.18).

Finally, we adapted the Clustering Model of Experiment 1 to the stimuli of Experiment 2. This was achieved analogously to the adaptation of the TSS Model. We implemented the stimulus-dependent color weight for both the first step (calculation of clusters) and the second step (cluster-based TSS) performed by the Clustering Model. The same functional relationship between color weight and color clustering in the stimulus which was calculated for the Color TSS Model led to optimal runlength values for the Clustering Model as well. The improvement of the Clustering Model achieved by its adjustment to color attributes turned out to be considerably smaller than for the TSS Model. We measured the similarity to the empirical scan paths in Experiment 2 for both the unadjusted Clustering Model and the new Color Clustering Model. While the Color Clustering Model produced results slightly more similar to the empirical paths (19.03) than those generated by the original Clustering Model (18.95), it could neither compete with the TSS Model nor with the Color TSS Model.

Figure 10 shows a survey of similarities between the models' paths and the empirical ones, in ascending order. Additionally, the values for the Greedy Model (17.25) and the optimum fit (20.65) are presented. A one-way analysis of variance showed a significant main effect, i.e. differences between the five models, $F(4; 76) = 65.74, p < 0.001$. Pairwise t-tests with Bonferroni-adjusted probabilities revealed that, as in Experiment 1, the Greedy heuristic yielded a significantly lower value than all other models, all $t(19) > 9.43, p < 0.001$. While there were no reliable differences between the Clustering Model, the Color Clustering Model, and the TSS Model, the Color TSS Model produced a significantly higher value than all its competitors, all $t(19) > 3.50, p < 0.024$.

4. General Discussion

Experiment 1 provided us with some fundamental insights into visual scanning strategies. First, the results suggest that the present scanning task does not induce any preferred direction for scanning, e.g. top to bottom or left to right. The reason might be that using a random distribution of items and a specified starting point makes this kind of schematic strategy rather inefficient. Second, the five

scan-path models differ substantially in their abilities to reproduce empirical scan paths. The TSS Model and the closely related Clustering Model yield clearly better results than their competitors, showing that the minimization of overall scan-path length might be an important determinant of human gaze trajectories. This does not imply that artificial neural networks are unable to generate human-like scan paths. Further research is necessary to determine adequate structures of neural networks for modeling human scanning behavior.

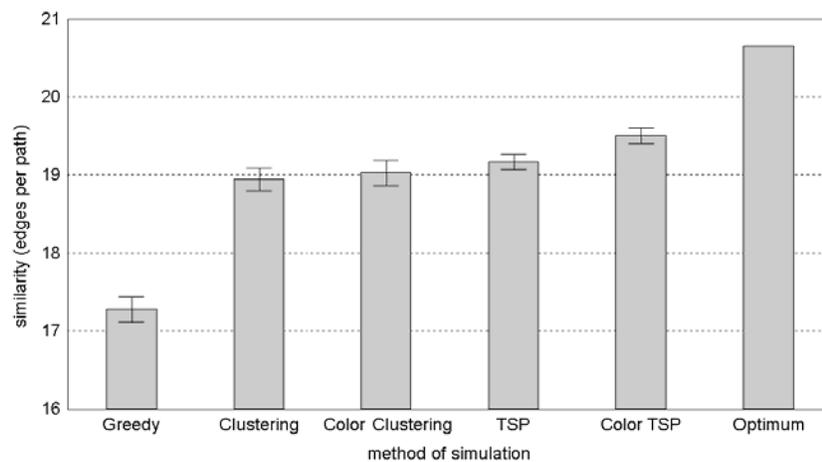


Figure 10. Similarity between the empirical scan paths of Experiment 2 and those yielded by the different models, plus the optimum fit path

Experiment 2 confirmed the results of Experiment 1. Moreover, it yielded information about the influence of color and form attributes on empirical scan paths. While viewers seem to ignore the forms of the items, they use the colors of the items in the scanning process, as demonstrated by disproportionately long color runs in their scan paths. The influence of color grows with increasing strength of color clustering in the stimulus. This color guidance is possibly employed to reduce memory load for generating self-avoiding scan paths. It requires less effort to keep in memory the clusters already visited and the items visited within the current cluster than to keep in memory the visited area of the

display on the basis of single items, especially if suitably large clusters are available. The perceptual grouping by form, however, does not seem to be strong enough to significantly influence the viewers' scanning strategies.

These results are in line with those obtained by Beckwith & Restle (1966), who found that clustering items by color or form reduced the time needed to count them, with color having a substantially stronger effect than form. Our findings are also compatible with eye-movement studies investigating saccadic selectivity in visual search tasks (e.g. Shen, Reingold, Pomplun & Williams, 2003; Williams & Reingold, 2001). Distractor items that are identical to the target in any dimension attract more fixations than others. Again, this effect is disproportionately large for the color dimension.

Conclusions concerning differences across dimensions, however, may not generalize beyond the set of items used in the experiment. In Experiment 2, other item sets, e.g. bars in different orientations, might have led to form-biased scan paths. Reducing the discriminability between colors would at some point have eliminated the influence of color on the scan paths. From the present data we can only confidently conclude that fully saturated colors affect scanning strategies, whereas regular geometrical forms do not.

Disproving our assumption, the effect of color on scan paths did not reduce their variability. The optimum fit value was actually lower in Experiment 2 (20.65) than in Experiment 1 (21.89), indicating higher differences between individual paths in Experiment 2 than in Experiment 1. This is probably due to the fact that, in Experiment 2, the effect of color varies considerably between individuals, which increases the range of applied strategies. The large standard error for relative color runlengths (see Figure 8) illustrates these individual differences.

Based on the empirically obtained color effect, the TSS and Clustering Models have been adapted to colored items. When using a weight for transitions between items of different colors to achieve this adaptation, this weight has to increase linearly with the strength of color clustering in the stimuli. Loosely speaking, the effect of color attributes on empirical scan paths seems to vary linearly with the amount of color clustering in the stimulus. We found the adaptation of the TSS Model – the Color TSS Model – to be a small but clear improvement over the standard TSS Model. The Color TSS Model is also superior

to the Clustering Model and its refined variant, the Color Clustering Model, and hence can be considered the “winner” of our competition.

Neither Experiment 1 nor Experiment 2 showed a significant difference in performance between the “color-blind” TSS and Clustering Models. Only the adaptation to colored items was achieved more effectively for the TSS Model. This does not mean that human viewers do not apply clustering strategies. In fact, the winning Color TSS Model performs clustering itself, since it fits its scan paths to the color clusters given in the stimulus. While this method of clustering could to some extent be adapted to human strategies, this could not be done with the more complex and less flexible algorithm used by the Clustering Model.

Altogether, the difficulties encountered in surpassing the plain TSS Model indicate that the geometrical optimization of scan paths, i.e., the minimization of their length, is the main common principle of human scanning strategies under the given task, even when additional color and form information is provided. Further research is needed to verify the applicability of the findings to real-world situations. For this purpose, stimuli could be photographs of real-world scenes – such as the breakfast scenes used by Rao and Ballard (1995) – and the task could be to memorize the scene, to detect a certain item, or to give a comprehensive verbal description (Clark & Krych, 2004; de Ruijter, Rossignol, Voorpijl, Cunningham & Levelt, 2003). Will scan-path minimization still be the dominant factor to determine the scan-path structure? Will the scanning strategies be influenced by the distribution of color and form attributes, by figural or functional interpretation, or by pragmatic considerations?

Answering these questions will be an important step towards understanding the principles our visual system employs when creating gaze trajectories. More generally, it will contribute to our understanding of human cognition in situated communication, where higher-level factors, visulinguistic processes, and communicative goals, strategies, and routines are to be taken into account (Garrod, Pickering & McElree, 2005; Rickheit, 2005). In this context, the present work can be viewed both as an intermediate step of import in the ongoing investigation of human cognition, and as a starting point for a promising line of research.

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