## 1 Exercises

Exercise 1. Consider inserting the following keys into an initially empty 2-3 search tree.

$$
\begin{array}{llllllllll}
\text { E } & \mathrm{A} & \mathrm{~S} & \mathrm{Y} & \mathrm{Q} & \mathrm{U} & \mathrm{~T} & \mathrm{I} & \mathrm{O} & \mathrm{~N}
\end{array}
$$

a. What is the height of the tree that results (assume root to be at height zero)? What is the minimum and maximum number of keys that a 2-3 search tree of this height can hold?
b. What are the 2-nodes in the tree?
c. What are the 3 -nodes in the tree?

Exercise 2. Suppose you insert the key 23 into the following left-leaning red-black BST:

a. Which of the following color flips result? Select all that apply.
A. Color flip 18
B. Color flip 22
C. Color flip 23
D. Color flip 24

E. Color flip 26
F. Color flip 28
b. Which of the following rotations result? Select all that apply.
A. Rotate 18 left
B. Rotate 18 right
C. Rotate 22 left
D. Rotate 22 right
E. Rotate 23 left
F. Rotate 23 right
G. Rotate 24 left

H. Rotate 24 right
I. Rotate 26 left
J. Rotate 26 right
K. Rotate 28 left
L. Rotate 28 right

## 2 Solutions to Exercises

## Solution 1.

a. 2; 7 and 14
b. (S), (U), (A), (Q), (T), (Y)
c. (E, O), (I, N)

## Solution 2.

a. E (Color flip 24)
b. A (Rotate 18 left), C (Rotate 22 left), J (Rotate 26 right), L (Rotate 28 right)

