

# **Data Structures and Algorithms in Java**

Sorting: Elementary (Bubble, Selection, Insertion, and Shell) Sorts

## Outline

- ① Prologue
- ② Selection Sort
- ③ Insertion Sort
- ④ Shell Sort

## Prologue

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Sorting is the process of arranging a sequence of objects in some logical order

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Example

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vonNeumann	3/26/2002	4121.85
Dijkstra	8/22/2007	2678.40
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Dijkstra	11/18/1995	837.42
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Hoare	8/18/1992	4381.21
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Turing	2/11/1991	2156.86
Hoare	8/12/2003	1025.70
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Dijkstra	9/10/2000	708.95
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Hoare	2/10/2005	4050.20

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## Prologue

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☰ dsa.Selection, dsa.Insertion, dsa.Shell, dsa.Merge, dsa.Quick, dsa.Quick3way, dsa.Heap

`static void sort(Comparable[] a)`

sorts the array `a` according to the natural order of its objects

`static void sort(Object[] a, Comparator c)`

sorts the array `a` according to the order induced by the comparator `c`

`static void sort(int[] a)`

sorts the array `a`

`static void sort(double[] a)`

sorts the array `a`

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A library  $\mathcal{L}$  that implements the sort API can sort (in ascending order) an array  $a$  of objects of type  $\tau$ , according to the objects' natural order, provided

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A library  $L$  that implements the sort API can sort (in ascending order) an array  $a$  of objects of type  $T$ , according to the objects' natural order, provided

- $T$  implements the `Comparable` interface
- If  $v$  and  $w$  are objects of type  $T$ , then `v.compareTo(w)` returns an integer that is negative, zero, or positive when  $v < w$ ,  $v = w$ , or  $v > w$ , respectively

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To sort  $a$ , we write

```
L.sort(a);
```

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- If  $v$  and  $w$  are objects of type  $T$  and  $c$  is an object of type `c`, then `c.compare(v, w)` returns an integer that is negative, zero, or positive when  $v < w$ ,  $v = w$ , or  $v > w$ , respectively

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To sort `a` using a comparator object `c`, we write

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L.sort(a, c);
```

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The sorting algorithms we consider refer to the objects they sort only through two operations: `less()` that compares two objects and `exchange()` that exchanges them

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A sorting algorithm is stable if it preserves the relative order of equal objects, ie, if  $i < j$  and  $a[i] \equiv a[j]$ , then  $\pi(i) < \pi(j)$ , where  $\pi(x)$  is the position of  $a[x]$  after the sort

## Prologue

Prologue

Example (transactions sorted by amount)

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```
>_ ~/workspace/dsaj/programs
```

```
$ _
```

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$ java dsa.XYZSort -
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```
$ java dsa.XYZSort -  
S o r t E x a m p l e  
<ctrl-d>
```

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S o r t E x a m p l e  
<ctrl-d>  
a E e l m o p r S t x  
$ -
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S o r t E x a m p l e  
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$ java dsa.XYZSort -  
S o r t E x a m p l e  
<ctrl-d>  
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```

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$ java dsa.XYZSort -  
S o r t E x a m p l e  
<ctrl-d>  
a E e l m o p r S t x  
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S o r t E x a m p l e  
<ctrl-d>
```

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S o r t E x a m p l e  
<ctrl-d>  
a E e l m o p r S t x  
$ java dsa.XYZSort +  
S o r t E x a m p l e  
<ctrl-d>  
E S a e l m o p r t x  
$ -
```



## Prologue

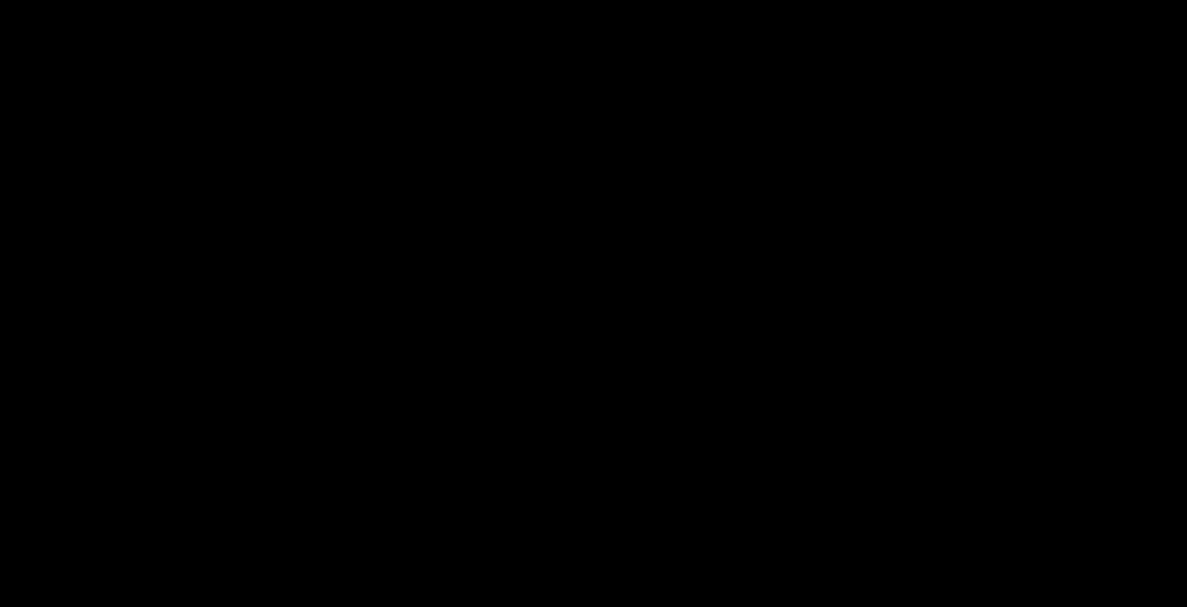
</> XYZSort.java

1/2

```
1 package dsa;
2
3 import java.util.Comparator;
4
5 import stdlib.StdIn;
6 import stdlib.StdOut;
7
8 public class XYZSort {
9     public static void sort(Comparable[] a) {
10         ...
11     }
12
13     public static void sort(Object[] a, Comparator c) {
14         ...
15     }
16
17     public static void sort(int[] a) {
18         ...
19     }
20
21     public static void sort(double[] a) {
22         ...
23     }
24
25     private static boolean less(Comparable v, Comparable w) {
26         return v.compareTo(w) < 0;
27     }
28
29     private static boolean less(Object v, Object w, Comparator c) {
30         return c.compare(v, w) < 0;
31     }
32
33     private static void exchange(Object[] a, int i, int j) {
34         Object swap = a[i];
35         a[i] = a[j];
```

```
36     a[j] = swap;
37 }
38
39 public static void main(String[] args) {
40     String[] a = StdIn.readAllStrings();
41     if (args[0].equals("-")) {
42         sort(a, String.CASE_INSENSITIVE_ORDER);
43     } else if (args[0].equals("+")) {
44         sort(a);
45     } else {
46         throw new IllegalArgumentException("Illegal command line argument");
47     }
48     for (String s : a) {
49         StdOut.print(s + " ");
50     }
51     StdOut.println();
52 }
53 }
```

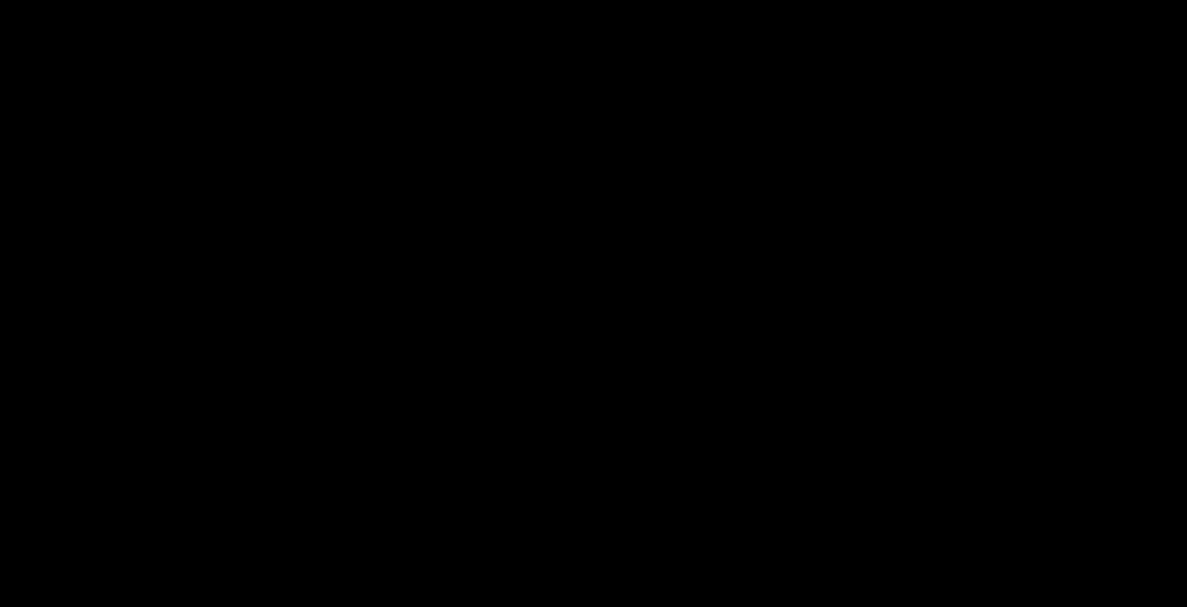
## Selection Sort



## Selection Sort

Find the smallest item in the array and exchange it with the first entry, then find the next smallest item and exchange it with the second entry, and so on

## Selection Sort



# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
		S	O	R	T	E	X	A	M	P	L	E

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
0	6	S	O	R	T	E	X	A	M	P	L	E



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# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
1	4	A	O	R	T	E	X	S	M	P	L	E

# Selection Sort

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i	min	0	1	2	3	4	5	6	7	8	9	10
1	4	A	E	R	T	O	X	S	M	P	L	E

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
2	10	A	E	R	T	O	X	S	M	P	L	E

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
2	10	A	E	E	T	O	X	S	M	P	L	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
3	9	A	E	E	T	O	X	S	M	P	L	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
3	9	A	E	E	L	O	X	S	M	P	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
4	7	A	E	E	L	O	X	S	M	P	T	R



# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
4	7	A	E	E	L	M	X	S	O	P	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
5	7	A	E	E	L	M	X	S	O	P	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
5	7	A	E	E	L	M	O	S	X	P	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
6	8	A	E	E	L	M	O	S	X	P	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
6	8	A	E	E	L	M	O	P	X	S	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
7	10	A	E	E	L	M	O	P	X	S	T	R

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
7	10	A	E	E	L	M	O	P	R	S	T	X

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
8	8	A	E	E	L	M	O	P	R	S	T	X



# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
8	8	A	E	E	L	M	O	P	R	S	T	X

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
9	9	A	E	E	L	M	O	P	R	S	T	X

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
9	9	A	E	E	L	M	O	P	R	S	T	X

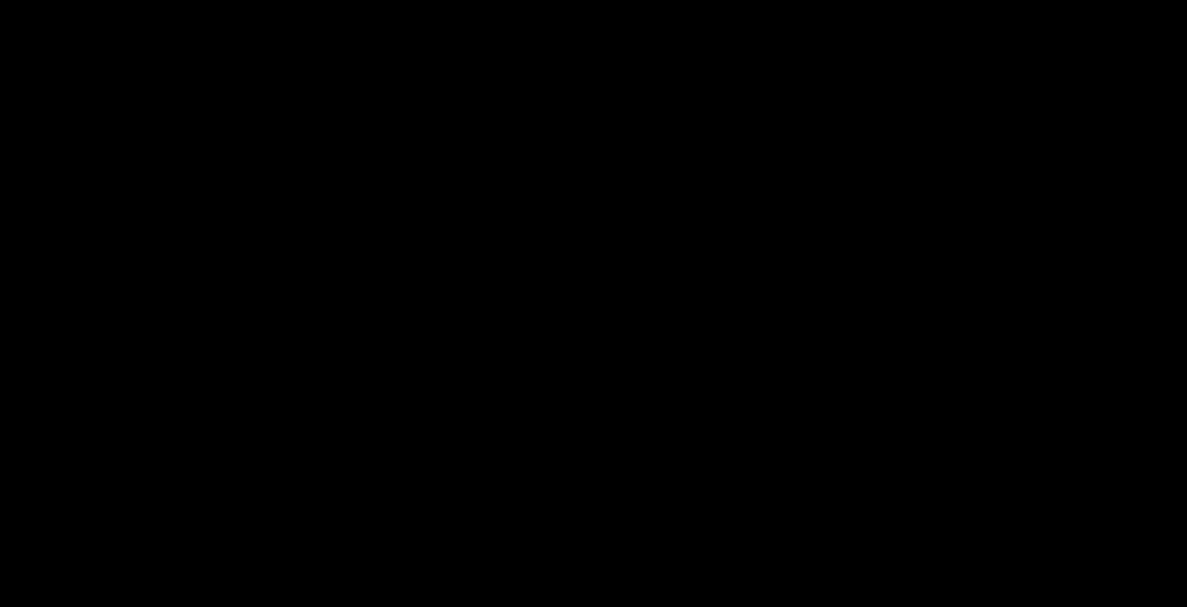
# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
10	10	A	E	E	L	M	O	P	R	S	T	X

# Selection Sort

		a[]										
i	min	0	1	2	3	4	5	6	7	8	9	10
10	10	A	E	E	L	M	O	P	R	S	T	X

## Selection Sort



## Selection Sort

</> Selection.java

```
1 public class Selection {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         for (int i = 0; i < n; i++) {
5             int min = i;
6             for (int j = i + 1; j < n; j++) {
7                 if (less(a[j], a[min])) {
8                     min = j;
9                 }
10            }
11            exchange(a, i, min);
12        }
13    }
14
15    public static void sort(Object[] a, Comparator c) {
16        int n = a.length;
17        for (int i = 0; i < n; i++) {
18            int min = i;
19            for (int j = i + 1; j < n; j++) {
20                if (less(a[j], a[min], c)) {
21                    min = j;
22                }
23            }
24            exchange(a, i, min);
25        }
26    }
27 }
```

## Selection Sort

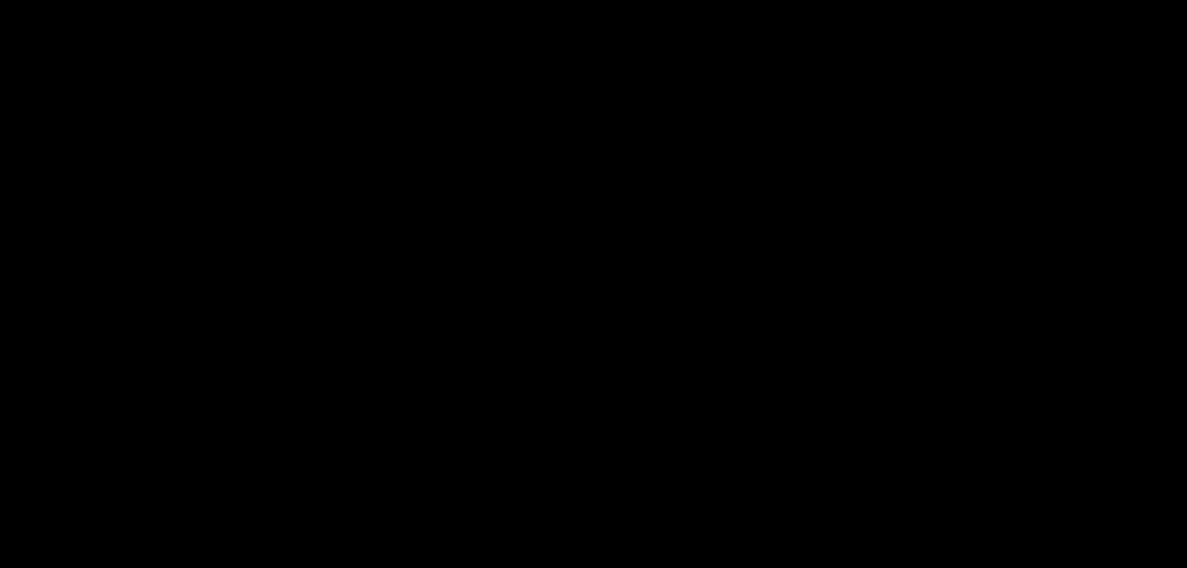
</> Selection.java

```
1 public class Selection {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         for (int i = 0; i < n; i++) {
5             int min = i;
6             for (int j = i + 1; j < n; j++) {
7                 if (less(a[j], a[min])) {
8                     min = j;
9                 }
10            }
11            exchange(a, i, min);
12        }
13    }
14
15    public static void sort(Object[] a, Comparator c) {
16        int n = a.length;
17        for (int i = 0; i < n; i++) {
18            int min = i;
19            for (int j = i + 1; j < n; j++) {
20                if (less(a[j], a[min], c)) {
21                    min = j;
22                }
23            }
24            exchange(a, i, min);
25        }
26    }
27 }
```

$$T(n) = n^2$$



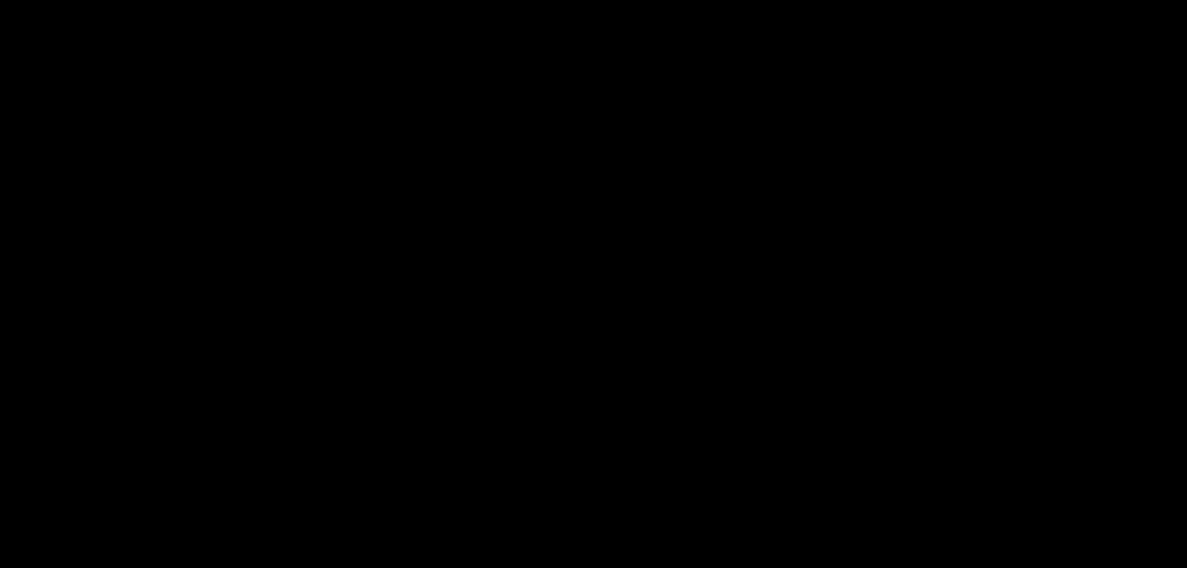
## Insertion Sort



## Insertion Sort

Consider the items one at a time, inserting each into its proper place among those already considered (ie, sorted)

## Insertion Sort



# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
		S	O	R	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
1	0	S	0	R	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
1	0	0	S	R	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
2	1	0	S	R	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
2	1	0	R	S	T	E	X	A	M	P	L	E



# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
3	3	0	R	S	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
3	3	0	R	S	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
4	0	0	R	S	T	E	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
4	0	E	O	R	S	T	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
5	5	E	O	R	S	T	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
5	5	E	O	R	S	T	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
6	0	E	O	R	S	T	X	A	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
6	0	A	E	O	R	S	T	X	M	P	L	E



# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
7	2	A	E	O	R	S	T	X	M	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
7	2	A	E	M	O	R	S	T	X	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
8	4	A	E	M	O	R	S	T	X	P	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
8	4	A	E	M	O	P	R	S	T	X	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
9	2	A	E	M	O	P	R	S	T	X	L	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
9	2	A	E	L	M	O	P	R	S	T	X	E

# Insertion Sort

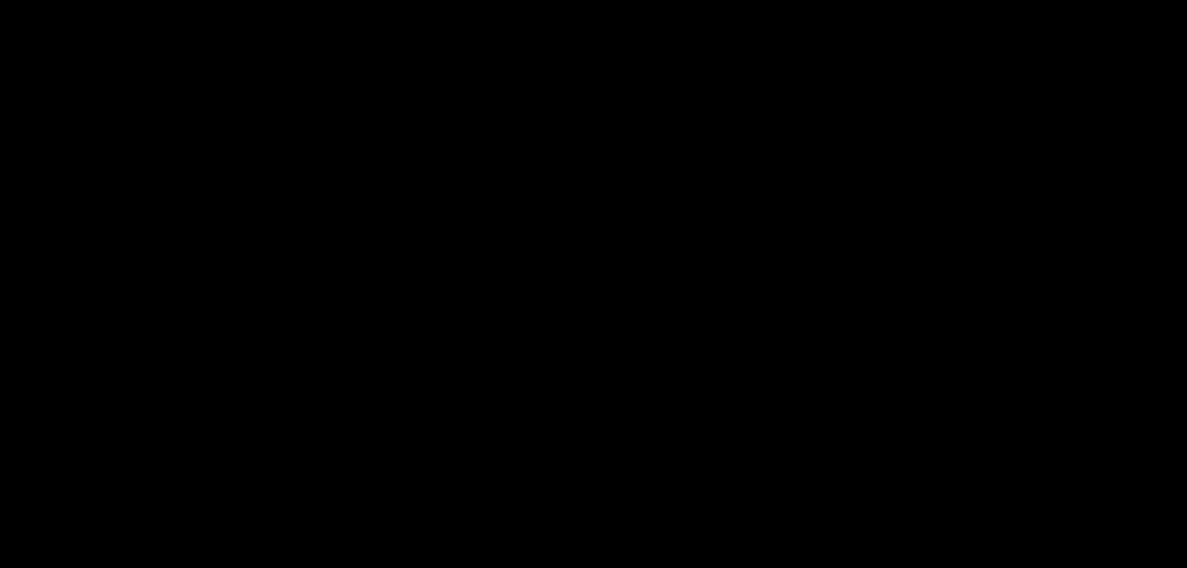
		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
10	2	A	E	L	M	O	P	R	S	T	X	E

# Insertion Sort

		a[]										
i	j	0	1	2	3	4	5	6	7	8	9	10
10	2	A	E	E	L	M	O	P	R	S	T	X



## Insertion Sort



## Insertion Sort

</> Insertion.java

```
1 public class Insertion {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         for (int i = 1; i < n; i++) {
5             for (int j = i; j > 0 && less(a[j], a[j - 1]); j--) {
6                 exchange(a, j, j - 1);
7             }
8         }
9     }
10
11    public static void sort(Object[] a, Comparator c) {
12        int n = a.length;
13        for (int i = 1; i < n; i++) {
14            for (int j = i; j > 0 && less(a[j], a[j - 1], c); j--) {
15                exchange(a, j, j - 1);
16            }
17        }
18    }
19 }
```

## Insertion Sort

</> Insertion.java

```
1 public class Insertion {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         for (int i = 1; i < n; i++) {
5             for (int j = i; j > 0 && less(a[j], a[j - 1]); j--) {
6                 exchange(a, j, j - 1);
7             }
8         }
9     }
10
11     public static void sort(Object[] a, Comparator c) {
12         int n = a.length;
13         for (int i = 1; i < n; i++) {
14             for (int j = i; j > 0 && less(a[j], a[j - 1], c); j--) {
15                 exchange(a, j, j - 1);
16             }
17         }
18     }
19 }
```

$$T(n) = n^2$$

## Shell Sort

## Shell Sort

Rearrange the array using insertion sort such that taking every  $k$ th entry (starting anywhere) yields a  $k$ -sorted subsequence

## Shell Sort

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
	S	H	E	L	L	S	O	R	T	E	X	A	M	P	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	S	H	E	L	L	S	O	R	T	E	X	A	M	P	L	E



# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	S	H	E	L	L	S	O	R	T	E	X	A	M	P	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
13	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	P	H	E	L	L	S	O	R	T	E	X	A	M	S	L	E



# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E



# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	H	E	L	P	S	O	R	T	E	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	L	P	H	O	R	T	S	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	L	P	H	O	R	T	S	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	L	P	H	O	R	T	S	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	L	P	H	O	R	T	S	X	A	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	P	H	O	L	T	S	X	R	M	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	P	H	O	L	T	S	X	R	M	S	L	E



# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	O	L	P	S	X	R	T	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	O	L	P	S	X	R	T	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	O	L	P	S	X	R	T	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	O	L	P	S	X	R	T	S	L	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	L	L	P	S	O	R	T	S	X	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	L	L	P	S	O	R	T	S	X	E

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4	L	E	E	A	M	H	L	E	P	S	O	L	T	S	X	R

# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	L	E	E	A	M	H	L	E	P	S	O	L	T	S	X	R



# Shell Sort

k	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	A	E	E	E	H	L	L	L	M	O	P	R	S	S	T	X

## Shell Sort

## Shell Sort

</> Shell.java

```
1 public class Shell {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         int k = 1;
5         while (k < n / 3) {
6             k = 3 * k + 1;
7         }
8         while (k >= 1) {
9             for (int i = k; i < n; i++) {
10                 for (int j = i; j >= k && less(a[j], a[j - k]); j -= k) {
11                     exchange(a, j, j - k);
12                 }
13             }
14             k /= 3;
15         }
16     }
17
18     public static void sort(Object[] a, Comparator c) {
19         int n = a.length;
20         int k = 1;
21         while (k < n / 3) {
22             k = 3 * k + 1;
23         }
24         while (k >= 1) {
25             for (int i = k; i < n; i++) {
26                 for (int j = i; j >= k && less(a[j], a[j - k], c); j -= k) {
27                     exchange(a, j, j - k);
28                 }
29             }
30             k /= 3;
31         }
32     }
33 }
```

## Shell Sort

</> Shell.java

```
1 public class Shell {
2     public static void sort(Comparable[] a) {
3         int n = a.length;
4         int k = 1;
5         while (k < n / 3) {
6             k = 3 * k + 1;
7         }
8         while (k >= 1) {
9             for (int i = k; i < n; i++) {
10                 for (int j = i; j >= k && less(a[j], a[j - k]); j -= k) {
11                     exchange(a, j, j - k);
12                 }
13             }
14             k /= 3;
15         }
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18     public static void sort(Object[] a, Comparator c) {
19         int n = a.length;
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21         while (k < n / 3) {
22             k = 3 * k + 1;
23         }
24         while (k >= 1) {
25             for (int i = k; i < n; i++) {
26                 for (int j = i; j >= k && less(a[j], a[j - k], c); j -= k) {
27                     exchange(a, j, j - k);
28                 }
29             }
30             k /= 3;
31         }
32     }
33 }
```

$T(n)$  not known (comparable to  $n \log n$ )