

## Lexical Analysis

## Outline

- 1 Scanning Tokens
- 2 Regular Expressions
- 3 Finite State Automata
- 4 Non-deterministic Versus Deterministic Finite State Automata
- 5 Regular Expressions to NFA
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## Scanning Tokens

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### Example

HelloWorld.java

```
// Copyright 2012- Bill Campbell, Swami Iyer and Bahar Akbal-Delibas
//
// Writes to standard output the message "Hello, World".

import java.lang.System;

public class HelloWorld {
    // Entry point.
    public static void main(String[] args) {
        System.out.println("Hello, World");
    }
}
```

Tokens: import, java, ., lang, ., System,;, public, class, HelloWorld, {, . . . , ;, }, }

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A scanner may be hand-crafted or generated from a specification consisting of regular expressions

## Scanning Tokens



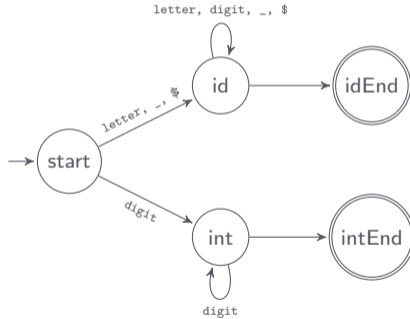
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A state transition diagram for recognizing identifiers and integers



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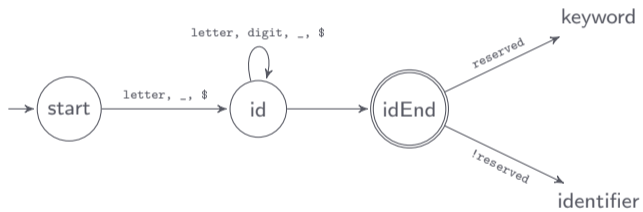
Scanner.java

```
if (isLetter(ch) || ch == '_' || ch == '$') {
    buffer = new StringBuffer();
    do {
        buffer.append(ch);
        nextCh();
    } while (isLetter(ch) || isDigit(ch) || ch == '_' || ch == '$');
    return new TokenInfo(IDENTIFIER, buffer.toString(), line);
} else if (isDigit(ch)){
    buffer = new StringBuffer();
    do {
        buffer.append(ch);
        nextCh();
    } while (isDigit(ch));
    return new TokenInfo(INT_LITERAL, buffer.toString(), line);
}
```

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A state transition diagram for recognizing keywords



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Scanner.java

```
reserved = new Hashtable<String, Integer>();
reserved.put("abstract", ABSTRACT);
reserved.put("boolean", BOOLEAN);
reserved.put("char", CHAR);
...
reserved.put("while", WHILE);

...

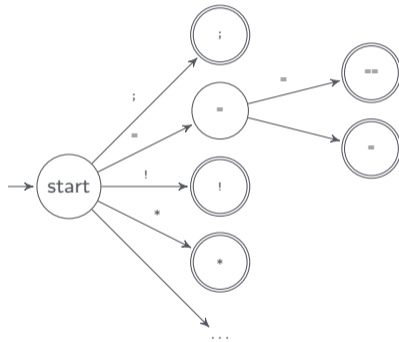
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    buffer = new StringBuffer();
    do {
        buffer.append(ch);
        nextCh();
    } while (isLetter(ch) || isDigit(ch) || ch == '_' || ch == '$');
    String identifier = buffer.toString();
    if (reserved.containsKey(identifier)) {
        return new TokenInfo(reserved.get(identifier), line);
    } else {
        return new TokenInfo(IDENTIFIER, identifier, line);
    }
}
```



## Scanning Tokens

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A state transition diagram for recognizing separators and operators



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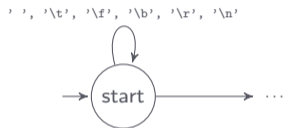
Scanner.java

```
switch (ch) {
    case ';':
        nextCh();
        return new TokenInfo(SEMI, line);
    case '=':
        nextCh();
        if (ch == '=') {
            nextCh();
            return new TokenInfo(EQUAL, line);
        } else {
            return new TokenInfo(ASSIGN, line);
        }
    case '!':
        nextCh();
        return new TokenInfo(LNOT, line);
    case '*':
        nextCh();
        return new TokenInfo(STAR, line);
    ...
}
```

## Scanning Tokens

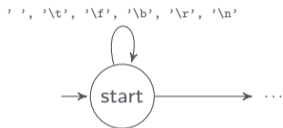
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Scanner.java

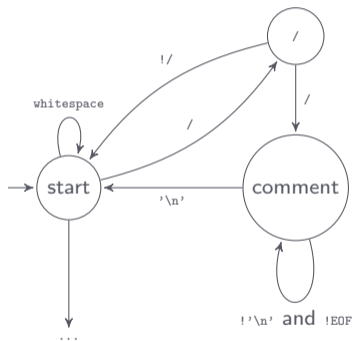
```
while (isWhitespace(ch)) {  
    nextCh();  
}
```

## Scanning Tokens



## Scanning Tokens

A state transition diagram for recognizing comments



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Scanner.java

```
boolean moreWhiteSpace = true;
while (moreWhiteSpace) {
    while (isWhitespace(ch)) {
        nextCh();
    }
    if (ch == '/') {
        nextCh();
        if (ch == '/') {
            while (ch != '\n' && ch != EOFCH) {
                nextCh();
            }
        } else {
            reportScannerError("Operator / is not supported in j--.");
        }
    } else {
        moreWhiteSpace = false;
    }
}
```

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Both  $r$  and  $(r)$  describe the same language, ie,  $L(r) = L((r))$

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- Integer literals may be described as

```
( "0"... "9" ) ( "0"... "9" )*
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- 5  $M$  is a set of moves (aka transitions) of the form  $m(r, a) = s$ , where  $r, s \in S$  and  $a \in \Sigma$

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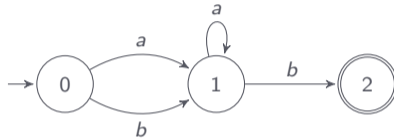
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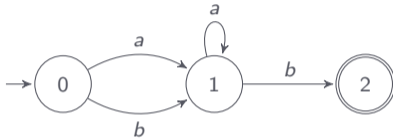




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Formally,  $F = (\Sigma, S, s_0, F, M)$ , where  $\Sigma = \{a, b\}$ ,  $S = \{0, 1, 2\}$ ,  $s_0 = 0$ ,  $F = \{2\}$ , and  $M$  is

$r$	$a$	$m(r, a)$
0	$a$	1
0	$b$	1
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A deterministic finite state automaton (DFA) is one in which:

- There are no  $\epsilon$ -moves
- There is a unique move from any state  $r$  on an input symbol  $a$ , ie, if  $m(r, a) = s$  and  $m(r, a) = t$ , then  $s = t$

## Non-deterministic Versus Deterministic Finite State Automata

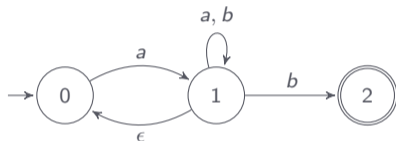
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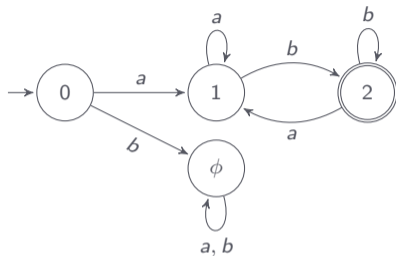
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$r$	$a$	$m(r, a)$
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And a DFA  $D$  that recognizes the same language



$D = (\Sigma, S, s_0, F, M)$  where  $\Sigma = \{a, b\}$ ,  $S = \{0, 1, 2, \phi\}$ ,  $s_0 = 0$ ,  $F = \{2\}$ , and  $M$  is

$r$	$a$	$m(r, a)$
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$\phi$	$a, b$	$\phi$

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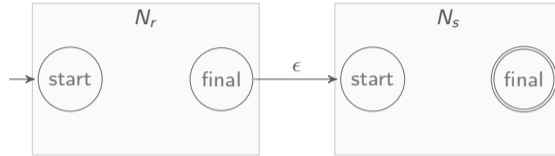
(Rule 2) NFA  $N_r$  for recognizing  $L(r = a)$



## Regular Expressions to NFA

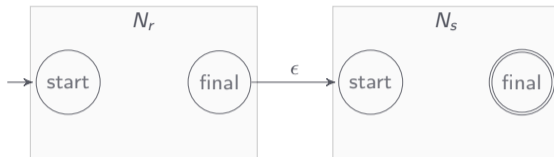
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(Rule 3) NFA  $N_{rs}$  for recognizing  $L(rs)$

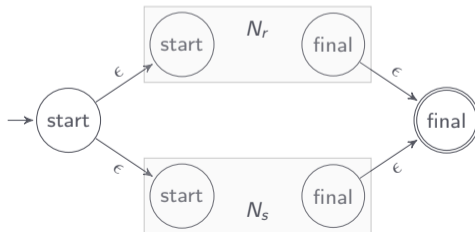


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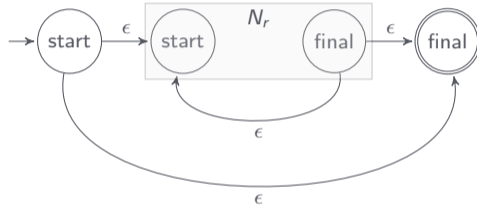
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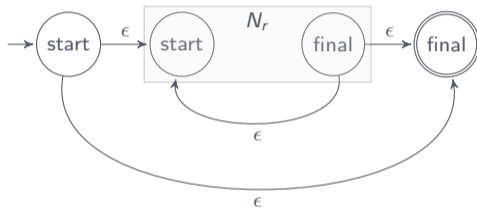
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(Rule 5) NFA  $N_{r^*}$  for recognizing  $L(r^*)$



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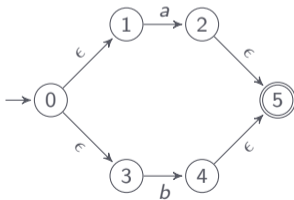
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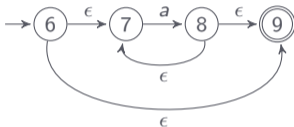
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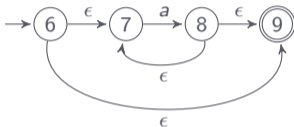


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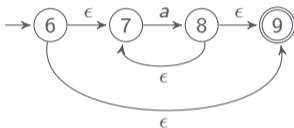
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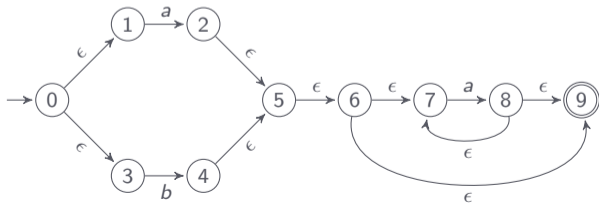
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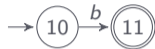
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Using Rule 2, we get the NFAs  $N_b$  for recognizing the second instance of  $b$  as



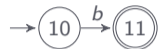
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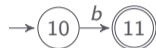
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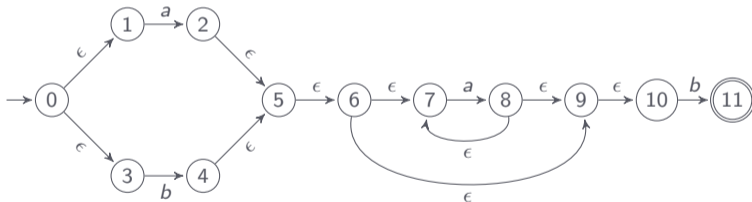
Finally, using Rule 3, we get the NFA  $N_{(a|b)a*b}$  for recognizing  $(a|b)a*b$  as

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## NFA to DFA

---

**Algorithm**  $\epsilon$ -closure( $S$ ) for a set of states  $S$

---

**Input:** a set of states  $S$

**Output:**  $\epsilon$ -closure( $S$ )

```
1:  $P \leftarrow \text{Stack}(S)$ 
2:  $C \leftarrow \text{Set}(S)$ 
3: while not  $P.\text{isEmpty}()$  do
4:    $r \leftarrow P.\text{pop}()$ 
5:   for  $s \in m(r, \epsilon)$  do
6:     if  $s \notin C$  then
7:        $P.\text{push}(s)$ 
8:        $C.\text{add}(s)$ 
9:     end if
10:  end for
11: end while
12: return  $C$ 
```

---

## NFA to DFA

---

**Algorithm**  $\epsilon$ -closure( $s$ ) for a state  $s$

---

**Input:** a state  $s$

**Output:**  $\epsilon$ -closure( $s$ )

1:  $S \leftarrow \text{Set}(s)$

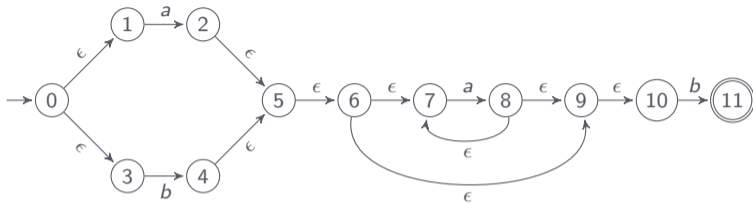
2: **return**  $\epsilon$ -closure( $S$ )

---

## NFA to DFA

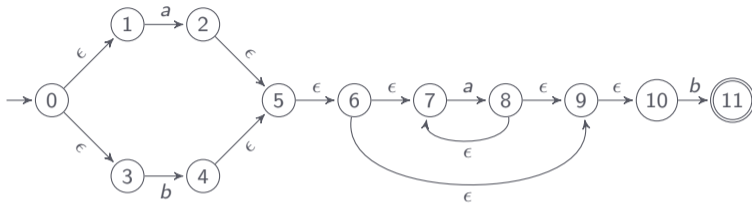
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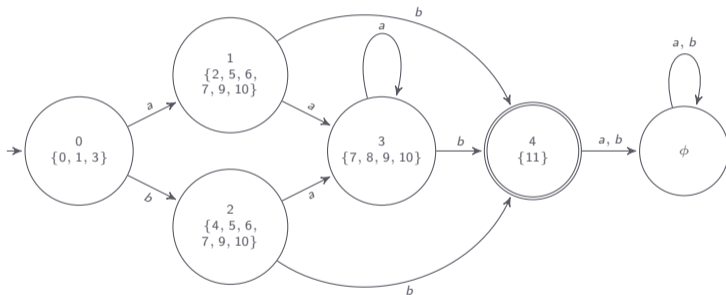
$r$	$a$	$m(r, a)$
$\{0, 1, 3\} = 0$ (start state)	$a$	$\{2, 5, 6, 7, 9, 10\} = 1$
0	$b$	$\{4, 5, 6, 7, 9, 10\} = 2$
1	$a$	$\{7, 8, 9, 10\} = 3$
1	$b$	$\{11\} = 4$ (accept state)
2	$a$	3
2	$b$	4
3	$a$	3
3	$b$	4
4	$a, b$	$\phi$
$\phi$	$a, b$	$\phi$



## NFA to DFA

## NFA to DFA

The DFA for recognizing  $(a|b)a^*b$



## NFA to DFA

---

## Algorithm NFA to DFA construction

---

**Input:** an NFA  $N = (\Sigma, S, s_0, M, F)$

**Output:** an equivalent DFA  $D = (\Sigma, S_D, s_{D0}, M_D, F_D)$

```
1:  $s_{D0} \leftarrow \epsilon\text{-closure}(s_0)$ 
2:  $S_D \leftarrow \text{Set}(s_{D0})$ 
3:  $M_D \leftarrow \text{Moves}()$ 
4:  $stk \leftarrow \text{Stack}(s_{D0})$ 
5:  $i \leftarrow 0$ 
6: while not  $stk.\text{isEmpty}()$  do
7:    $r \leftarrow stk.\text{pop}()$ 
8:   for  $a \in \Sigma$  do
9:      $s_{Di+1} \leftarrow \epsilon\text{-closure}(m(r, a))$ 
10:    if  $s_{Di+1} \neq \{\}$  then
11:      if  $s_{Di+1} \notin S_D$  then
12:         $S_D.\text{add}(s_{Di+1})$ 
13:         $stk.\text{push}(s_{Di+1})$ 
14:         $i \leftarrow i + 1$ 
15:         $M_D.\text{add}((r, a) \rightarrow s_{Di+1})$ 
16:      else if  $\exists s_j \in S_D$  such that  $s_{Di+1} = s_j$  then
17:         $M_D.\text{add}((r, a) \rightarrow s_j)$ 
18:      end if
19:    end if
20:  end for
21: end while
22:  $F_D \leftarrow \text{Set}()$ 
23: for  $s_D \in S_D$  do
24:   for  $s \in s_D$  do
25:    if  $s \in F$  then
26:       $F_D.\text{add}(s_D)$ 
27:    end if
28:  end for
29: end for
30: return  $D = (\Sigma, S_D, s_{D0}, M_D, F_D)$ 
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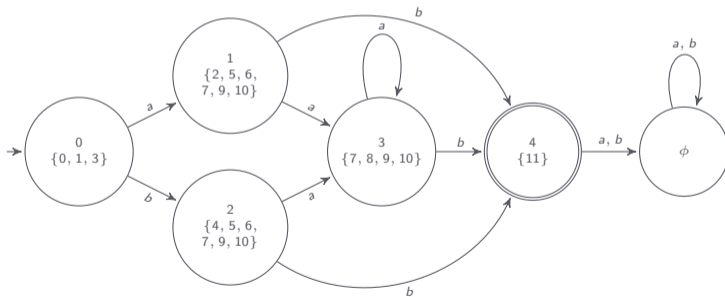
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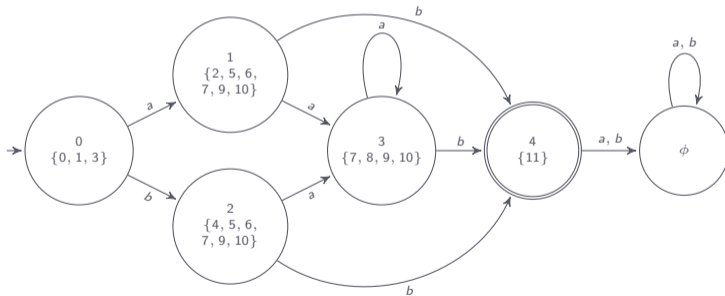


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For example, consider the DFA for  $(a|b)a*b$



The initial partition contains the subsets  $\{0, 1, 2, 3, \phi\}$  and  $\{4\}$

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The symbol  $a$  does not split the subset  $\{0, 1, 2, 3, \phi\}$ , since

$$m(0, a) = 1$$

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The symbol  $b$  splits the subset  $\{0, 1, 2, 3, \phi\}$  into subsets  $\{0, \phi\}$  and  $\{1, 2, 3\}$ , since

$$m(0, b) = 2$$

$$m(1, b) = 4$$

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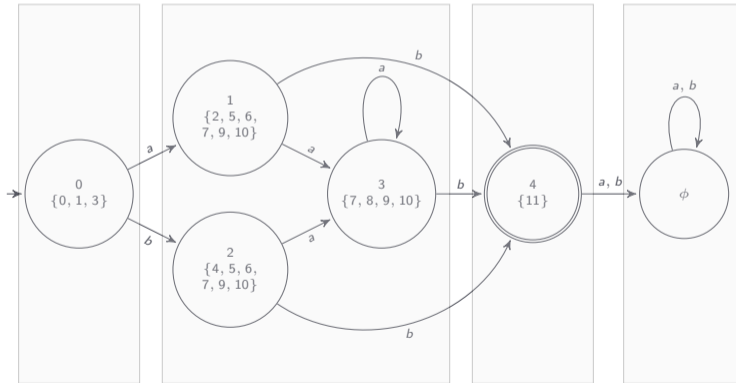


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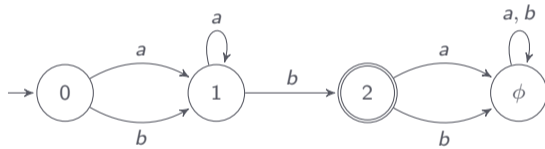
The final partition is therefore  $\{\{0\}, \{1, 2, 3\}, \{4\}, \{\phi\}\}$



## DFA to Minimal DFA

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Minimal DFA for recognizing  $(a|b)a^*b$



## DFA to Minimal DFA

## DFA to Minimal DFA

---

### Algorithm Minimizing a DFA

---

**Input:** a DFA  $D = (\Sigma, S, s_0, M, F)$

**Output:** a partition of  $S$

```
1:  $partition \leftarrow \{S - F, F\}$ 
2: while splitting occurs do
3:   for  $subset \in partition$  do
4:     if  $subset.size() > 1$  then
5:       for  $a \in \Sigma$  do
6:          $r \leftarrow$  a state chosen from  $subset$ 
7:          $targetSet \leftarrow$  the subset in the partition containing  $m(r, a)$ 
8:          $set1 \leftarrow \{s \in subset \mid m(s, a) \in targetSet\}$ 
9:          $set2 \leftarrow \{s \in subset \mid m(s, a) \notin targetSet\}$ 
10:        if  $set2 \neq \{\}$  then
11:          replace  $subset$  in  $partition$  by  $set1$  and  $set2$ 
12:          break
13:        end if
14:      end for
15:    end if
16:  end for
17: end while
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After a match, the scanner goes into a specified state or stays in the current state



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JavaCC generates a scanner for `j--` from regular expressions defined in `$j/j--/src/jminusminus/j--.jj`





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}
```

## Scanning reserved words, separators, and operators

```
TOKEN: {  
  <ABSTRACT: "abstract">  
  | <BOOLEAN: "boolean">  
  ...  
  | <COMMA: ",">  
  | <DOT: "." >  
  ...  
  | <ASSIGN: "=">  
  | <DEC: "--">  
  ...  
}
```





## Scanning identifiers

```
TOKEN: {  
  <IDENTIFIER: ( <LETTER> | "_" | "$" ) ( <LETTER> | <DIGIT> | "_" | "$" )*>  
  | <#LETTER: [ "a"- "z", "A"- "Z" ]>  
  | <#DIGIT: [ "0"- "9" ]>  
}
```

## Scanning identifiers

```
TOKEN: {  
  <IDENTIFIER: ( <LETTER> | "_" | "$" ) ( <LETTER> | <DIGIT> | "_" | "$" )*>  
  | <#LETTER: [ "a"- "z", "A"- "Z" ]>  
  | <#DIGIT: [ "0"- "9" ]>  
}
```

## Scanning literals

```
TOKEN: {  
  <INT_LITERAL: <DIGIT> ( <DIGIT> )*>  
  | <CHAR_LITERAL: ">" ( <ESC> | ~[ ">", "\\> ] ) ">">  
  | <STRING_LITERAL: "\" ( <ESC> | ~[ "\" , "\\> ] )* "\">  
  | <#ESC: "\\> [ "n", "t", "b", "r", "f", "\\>, ">, "\" ]>  
}
```