

UMass Boston Computer Science
CS450 High Level Languages

Programming with Compound Data

Thursday, February 19, 2026

```
class Horse  
  implements Animal {  
    Int age;  
    Float weight;  
  }
```



Logistics

- HW 3 out
 - due: Tues 2/24 11am EST
 - Similar to HW 2, but with compound data defs (start from scratch!)
- New Office Hour Time
 - Thurs 2-3:30pm

(OO languages love compound data)

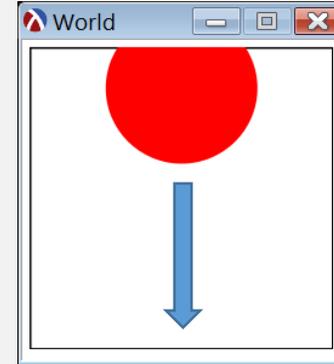
```
class Horse
  implements Animal {
    Int age;
    Float weight;
  }
```



Last
Time

Falling "Ball" Example

```
;; A WorldState is a Non-negative Integer  
;;           Represents: the y Coordinate of the center of a  
;;           ball in a `big-bang` animation.
```



← What if ... the ball can also move side-to-side?? →

WorldState would need two pieces of data:
the *x* and *y* coordinates

```
;; A WorldState is an Integer ...  
;; ... and another Integer???
```

We need a way to create **compound data**
i.e., a **data definition** that
combines values of other data defs

Last
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Kinds of Data Definitions

- **Basic data**
 - E.g., numbers, strings, etc
- **Intervals**
 - Data that is from a range of values, e.g., $[0, 100)$
- **Enumerations**
 - Data that is one of a list of possible values, e.g., “green”, “red”, “yellow”
- **Itemizations**
 - Data value that can be from a list of possible other data definitions
 - E.g., either a string or number (Generalizes enumerations)
- ➔ • **Compound Data**
 - Data that is a combination of values from other data definitions

Last
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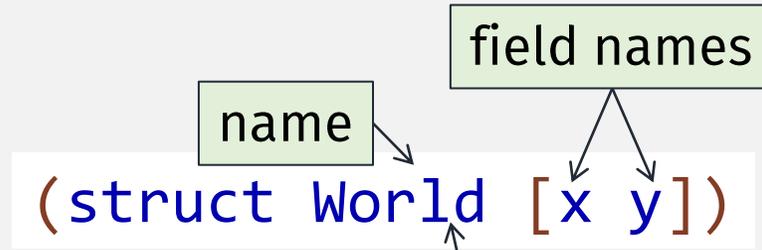
Falling “Ball” Example

a struct defines a
new kind of
compound data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])  
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y)  
;; ...
```

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Parts of a **struct** definition



(Implicitly) defines:

• A **constructor** function \longrightarrow `World`

- Creates instances of the struct

• **Accessor** functions \longrightarrow `World-x`, `World-y`

- Get an instance's field value

• A **predicate** \longrightarrow `World?`

- Returns true for struct instances

"name" + "-" + ...

... field names

"name" + "?"

Last
Time

Falling "Ball" Example

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])  
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))  
;; ...
```

a struct defines a
new kind of
compound data

Checked constructor
(programmer must define)

Unchecked (internal) constructor
(implicitly defined by struct)

```
(define INIT-WORLDSTATE (mk-WorldState 0 0))
```

Produces **instances** of the
struct that are **values** of the
new data definition

Data Design Recipe

Data Definition

- Has 4 parts:
 1. **Name**
 2. Description of **all possible values** of the data
 3. **Interpretation** explaining the real world concepts the data represents
 4. **Predicate** returning **false** for (most?) values not in the Data Definition
 - If needed, define extra predicates for each **enumeration** or **itemization**

Data Design Recipe - Compound Data Update

Data Definition (for compound data)

• ~~Has 4~~ Has 5 parts:

1. **Name**
2. Description of **all possible values** of the data
3. **Interpretation** explaining the real world concepts the data represents
4. **Predicate** returning **false** for (most?) values not in the Data Definition
 - If needed, define extra predicates for each **enumeration** or **itemization**
- ➔ 5. (checked) **Constructor** for **compound data def values**

Data Design Recipe - Compound Data Predicate

Data Definition (for compound data)

- Has 5 parts:
 1. **Name**
 2. Description of **all possible values** of the data
 3. **Interpretation** explaining the real world concepts the data represents
 - ➔ 4. **Predicate** returning **false** for (most?) values not in the **Data Definition**
 - For compound data ...
 5. (checked) **Constructor** for compound data def values

Predicates for Compound Data

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])  
;; Represents: coordinate in big-bang animation where:  
;; - x is ball (red solid circle) horizontal center  
;; - y is ball vertical center  
(struct World [x y])
```

predicate?

struct already defines World? ...
but does not enforce field types?

```
(define (WorldState? arg)  
  (and (World? arg)  
        (integer? (World-x arg))  
        (integer? (World-y arg))))
```

???

This “deep” predicate checks too much...

... because it’s the job of “field data type” processing functions to check those kinds of data

Also not practical? maybe exponential overhead ...

Compound data predicates
should be “**shallow**” checks, i.e., World?

Instead, use **checked constructor**: ensures that only valid instances are created!

```
(define/contract (mk-WorldState x y)  
  (-> integer? integer? WorldState?)  
  (World x y))
```

Data Design Recipe - Predicate Update

Data Definition (for compound data)

- Has 5 parts:
 1. **Name**
 2. Description of **all possible values** of the data
 3. **Interpretation** explaining the real world concepts the data represents
 4. **Predicate** (shallow, conservative approximation of the Data Def)
 - Evaluates to **true** for all values in the Data Def ... and maybe some not
 - False positives maybe **ok** Might let in some invalid values
 - Evaluates to **false** for (most?) values not in the Data Def ... but maybe not all
 - False negatives **not ok** Must only reject invalid values
 5. (checked) **Constructor** for compound data def values

Function Design Recipe

1. **Name**
2. **Signature** – types of the function input(s) and output
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using `check-equal?`) the function behavior
5. **Template** – sketch out the function structure (using input's Data Definition)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using `check-equal?` and other test forms) the function behavior

Functions For Compound Data

- A function that processes compound data must ...
 - extract the individual pieces, using accessors
 - combine them, with arithmetic

Functions For Compound Data - Template

- A function that processes compound data must
 - extract the individual pieces, using accessors ←
 - combine them, with arithmetic

Done with template

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])

(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?)
  (World x y))
```

```
;; TEMPLATE for WorldState-fn: WorldState -> ???
(define (WorldState-fn w)

  .... (World-x w) ....
  .... (World-y w) .... )
```

A function's
template is
completely
determined by
the input's
Data Definition

Functions For Compound Data - Template

- A function that processes compound data must
 - extract the individual pieces, using accessors ←
 - combine them, with arithmetic

Done with template

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])

(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?)
  (World x y))
```

```
;; TEMPLATE for WorldState-fn: WorldState -> ???
(define/contract (WorldState-fn w)
  (-> WorldState? ??? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

A function's
template is
completely
determined by
the input's
Data Definition

Function Design Recipe

Still must program with these steps,
in this order!

1. **Name**
2. **Signature** – types of the **function input(s)** and **output** (not submitted in comments, if there are valid **contracts**)
3. **Description** – explain (in English prose) the function behavior
4. **Examples** – show (using `check-equal?`) the function behavior
5. **Template** – sketch out the function structure (using input's Data Definition) (not submitted)
6. **Code** – implement the rest of the function (arithmetic)
7. **Tests** – check (using `check-equal?` and other test forms) the function behavior

```
;; A WorldState is a (mk-WorldState [x : Int] [y : Int])
(struct World [x y])

(define/contract (mk-WorldState x y)
  (-> integer? integer? WorldState?)
  (World x y))
```

```
(check-equal?
  (next-WorldState
    (mk-WorldState 0 0))
  (mk-WorldState X-VEL Y-VEL))
```

(assuming constant velocity)

```
;; next-WorldState : WorldState -> WorldState
;; Computes the ball position after 1 tick
```

```
;; TEMPLATE for WorldState:
(define/contract (WorldState-fn w)
  (-> WorldState? ??? )
  .... (World-x w) ....
  .... (World-y w) .... )
```

```
(check-equal?
  (next-WorldState
    (mk-WorldState 0 0))
  (mk-WorldState X-VEL Y-VEL))
```

```
;; next-WorldState
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)
  (-> WorldState? WorldState?)
  .... (World-x w) ....
  .... (World-y w) .... )
```

```
;; next-WorldState  
;; Computes the ball position after 1 tick
```

```
(define/contract (next-WorldState w)  
  (-> WorldState? WorldState?)  
  (mk-WorldState  
    (+ (World-x w) X-VEL)  
    (+ (World-y w) Y-VEL)))
```

```
(check-equal?  
  (next-WorldState  
    (mk-WorldState 0 0))  
  (mk-WorldState X-VEL Y-VEL))
```

Example + Template helps
to write the function!

Extract Compound Pieces – **let**

alternatives

See also **let***

```
(define/contract (next-WorldState w)
```

; ...

```
(let ([x (World-x w)]  
      [y (World-y w)]))
```

Defines new local variables

```
(mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

in scope only in the body

Extract all compound data pieces first, before doing “arithmetic”

```
(let ([id val-expr] ...) body ...+)
```

Local variables shadow previously defined vars

Extract Compound Pieces – (internal) **define**

alternatives

```
(define/contract (next-WorldState w)
```

```
; ...
```

```
(define x (World-x w))
```

```
(define y (World-y w))
```

```
(mk-WorldState (+ x X-VEL) (+ y Y-VE
```

Extract all compound data pieces first, before doing “arithmetic”

(is there an easier way to do this?)

Extract Compound Pieces – Pattern Match!

alternatives

```
(define/contract (next-WorldState w)
```

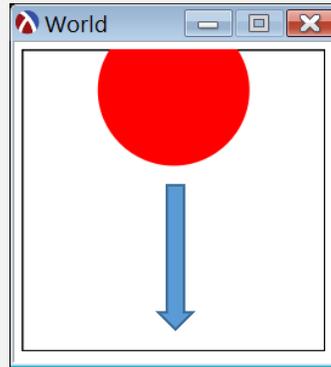
```
; ...
```

```
(match-define (World x y) w)
```

```
(mk-WorldState (+ x X-VEL) (+ y Y-VEL))))
```

Extract all compound
data pieces, at the
same time!

Falling “Ball” Example



← What if the **ball** can also move side-to-side ... →

... on a key-press?

`WorldState` would need two pieces of data:
the *x* and *y* coordinates

Last Time

Some Pre-defined Enumerations

```

; A KeyEvent is one of:
; - 1String
; - "left"
; - "right"
; - "up"
; ...

```

"KeyEvent" function

... cannot do "WorldState" function "things"!

(result must be **WorldState**)

But remember:

1 function does 1 task which processes 1 kind of data

WorldState

Give to: **big-bang on-key** clause

Must call separate: "WorldState fn"

... to do "WorldState" function "things"

Template

```

; WorldState KeyEvent -> ..
(define (handle-key-events w ke)
  (cond
    [(= (string-length ke) 1) ...]
    [(string=? "left" ke) .. (handle-left w) ???]
    [(string=? "right" ke) . (handle-right w) ???]
    [(string=? "up" ke) ...]
    [(string=? "down" ke) ...]
    ...))

```

Or even better: **key=?**

Do not put all code in one function! e.g., Do not process "WorldState" data in a "KeyEvent" function!

Compound Data can be nested

But remember:

1 function does
1 task which processes
1 kind of data

Need a different function (that uses GameState template) to process GameState data

Uses KeyEvent template

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    [(key=? k GET-RED) (handle-red-key g) ]
    [(key=? k GET-BLUE) (handle-blue-key g) ]
    [else w]))
```

Compound Data can be nested

But remember:

1 function does
1 task which processes
1 kind of data

Makes testing easier! →

```
(check-equal? (key-handler ANY-GAMESTATE "r")  
              (handle-red-key ANY-GAMESTATE))  
(check-equal? (key-handler ANY-GAMESTATE "b")  
              (handle-blue-key ANY-GAMESTATE))
```

(but still need some "full stack" tests)

```
(define/contract (key-handler g k)  
  (-> GameState? key-event? GameState?)  
  (cond  
    [(key=? k GET-RED) (handle-red-key g)]  
    [(key=? k GET-BLUE) (handle-blue-key g)]  
    [else w]))
```

Function Design Recipe - Testing Update

- “Full Stack”

- For “top level” functions
- Tests: all functionality from input to final result
- Should be more comprehensive

```
(check-equal? (key-handler SOME-GAMESTATE1 "r")  
              NEXT-GAMESTATE2)  
(check-equal? (key-handler SOME-GAMESTATE3 "b")  
              NEXT-GAMESTATE4)
```

- “Incremental”

- For “helper” (and top level) functions
- Tests: more local functionality – dictated by data design
- delegate to other helpers, should test “control flow” paths

```
(check-equal? (key-handler ANY-GAMESTATE "r")  
              (handle-red-key ANY-GAMESTATE))  
(check-equal? (key-handler ANY-GAMESTATE "b")  
              (handle-blue-key ANY-GAMESTATE))
```

A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

TEMPLATE

(extracts pieces of compound data)

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... ))
```

Look at type(s) to help fill in template

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-red-key g)
  (-> GameState? GameState?)
  (mk-GameState
    (Player-fn (GameState-p1 g))
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)  
;; (mk-GameState [p1 : Player] [p2 : Player]  
;;              [active : PlayerID])  
  
;; where:  
;; - p1 : represents “Player 1” data ...  
;; - p2 : represents “Player 2” data ...  
;; - active : it’s this player’s turn
```

NOTE: don’t “prematurely optimize!”

Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs... We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil.

— Donald Knuth

```
(define/contract (handle-red-key g)  
  (-> GameState? GameState?)  
  (mk-GameState  
    (Player-fn (GameState-p1 g) (GameState-p2 g) (GameState-active g))  
    (Player-fn (GameState-p2 g) (GameState-p1 g) (GameState-active g))  
    (PlayerID-fn (GameState-active g) (GameState-p1 g) (GameState-p2 g))))
```

(can always refactor to be “cleaner” later)

Pass as many compound data pieces as needed ...

(trust the recipe ... follow the data design ... resist temptation to “prematurely optimize”)

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])

;; where:
;; - p1 : represents "Player 1" data ...
;; - p2 : represents "Player 2" data ...
;; - active : it's this player's turn
(struct GameState [p1 p2 active])
```

```
;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS
```

```
;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS
```

"invariant" = "must always be true!"

Previously

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState?)
  (GameState p1 p2 id))
```

Can these be "any" Player values?

```
;; A Player is a Assume hypothetically ...
;; (mk-Player [red : TokenCount]
;;            [blue : TokenCount])
```

Every function that creates a GameState is responsible for maintaining its invariants!

Can this be automatically checked?

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])

;; where:
;; - p1 : represents "Player 1" data ...
;; - p2 : represents "Player 2" data ...
;; - active : it's this player's turn
(struct GameState [p1 p2 active])
```

Every function that creates a GameState is responsible for maintaining its invariants!

```
;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS
```

Can this be automatically checked?

```
;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS
```

One possibility:
define a separate "output" predicate

With Invariant Check

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState/invariant?)
  (GameState p1 p2 id))
```

```
(define (GameState/invariant? x)
  (and (GameState? x)
        (<= (+ (red-count (GameState-p1 x))
                (red-count (GameState-p2 x)))
            MAX-TOKENS)
        (<= (+ (blue-count (GameState-p1 x))
                (blue-count (GameState-p2 x)))
            MAX-TOKENS))))
```

Data Definition Invariants

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player
                             [active : PlayerID])

;; where:
;; - p1 : represents "Player 1" data ...
;; - p2 : represents "Player 2" data ...
;; - active : it's this player's turn
(struct GameState [p1 p2 active])
```

```
;; Invariant1: p1 "red" + p2 "red" <= MAX-TOKENS
```

```
;; Invariant2: p1 "blue" + p2 "blue" <= MAX-TOKENS
```

```
(define/contract (mk-GameState p1 p2 id)
  (-> Player? Player? PlayerID? GameState/invariant?)
  (GameState p1 p2 id))
```

But remember:

- compound data contracts should be "shallow"
- i.e., don't traverse an entire (nested) data structure
- Programmer must decide what is "too deep"

This one probably ok because ...
still "constant" time check

Every function that creates a
GameState is responsible for
maintaining its invariants!

"Dependent"
Contract

Can this be automatically checked?

One possibility:
define a separate "output" predicate

```
(define (GameState/invariant? x)
  (and (GameState? x)
       (GameState-red-invariant? x)
       (GameState-blue-invariant? x)))
```

(with better-named helper functions!
Avoid large unreadable boolean
expressions!)

Data Design Recipe - Predicate Update

Data Definition (for compound data)

- Has 5 parts:
 1. **Name**
 2. Description of **all possible values** of the data
 3. **Interpretation** explaining the real world concepts the data represents
 4. **Predicate** (shallow, conservative approximation of the Data Def)
 - Evaluates to **true** for all values in the Data Def, and maybe some not
 - False positives maybe **ok** Might let in some invalid values
 - Evaluates to **false** for (most?) values not in the Data Def, but maybe not all
 - False negatives **not ok** Must only reject invalid values
 5. (checked) **Constructor** for compound data def values
- ➔ • Consider “dependent” “output” contracts ... to check **invariants**

Follow data definitions whenever possible, but ...

Sometimes you need “**if**” ... ?

```
(define/contract (key-handler g k)
  (-> GameState? key-event? GameState?)
  (cond
    . . . .
    [(key=? k SPEND-KEY) (handle-spend g)]
    . . . .
    [else w]))
```

a “GameState” function!

A “GameState” data def + function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (GameState-fn g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

TEMPLATE

(extracts pieces of compound data)

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? .... )

  .... (GameState-p1 g) ....
  .... (GameState-p2 g) ....
  .... (GameState-active g) .... )
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;              [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... ))
```

Look at type(s) to help fill in template

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    .... (GameState-p1 g) ....
    .... (GameState-p2 g) ....
    .... (GameState-active g) .... ))
```

A “GameState” function ...

```
;; A GameState is a (hypothetically ...)
;; (mk-GameState [p1 : Player] [p2 : Player]
;;               [active : PlayerID])
;; where:
;; - p1 : represents “Player 1” data ...
;; - p2 : represents “Player 2” data ...
;; - active : it’s this player’s turn
```

But remember:

**1 function does
1 task which processes
1 kind of data**

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
    (Player-fn (GameState-p1 g))
    (Player-fn (GameState-p2 g))
    (PlayerID-fn (GameState-active g))))
```

Don’t do “Player” function “things” in a “GameState” function!

A “GameState” function needs “Player” fn

```
(define/contract (handle-spend g)
  (-> GameState? GameState?)
  (mk-GameState
   (player-spend (GameState-p1 g)) (assuming this is “active” player)
   (Player-fn (GameState-p2 g))
   (PlayerID-fn (GameState-active g))))
```

A “Player” function ...

```
;; A Player is a Assume hypothetically ...  
;; (mk-Player [red : TokenCount]  
;;           [blue : TokenCount])
```

```
(define/contract (player-fn p)  
  (-> Player? ....)  
  
  .... (Player-red p) ....) (template)  
  .... (Player-blue p) ....))
```

A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here ... because we don’t want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (mk-Player
   (spend-token (Player-red p))
   (spend-token (Player-blue p))))
```

(from hw1)

A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

(not great)
Don't write this!

No giant boolean expressions!

“Dependent” contract won't suffice here ... because we don't want to error

We really need “if”!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (and (not (zero? (Player-red p)))
           (not (zero? (Player-blue p))))
      (mk-Player
       (spend-token (Player-red p))
       (spend-token (Player-blue p)))
```

A “Player” function ...

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here ... because we don’t want to error

We really need “if”!

(not great)
Don’t write this!

Name doesn’t accurately describe what the function does!

```
(define/contract (player-spend p)
  (-> Player? Player?)
  (if (can-spend? .... )
      (mk-Player
        (spend-token (Player-red p))
        (spend-token (Player-blue p)))
      )
  )
```

A “Player” function ...

Write this!

Name accurately describes what the function does!

```
(define/contract (player-maybe-spend p)
  (-> Player? Player?)
  (if (can-spend? p)
      (player-spend p)
      p))
```

Are there any invariants to maintain?

Player should only “spend” if they have sufficient tokens, e.g., 1 red and 1 blue

“Dependent” contract won’t suffice here ... because we don’t want to error

We really need “if”!

Function Design Recipe - “**if**” edition

- Avoid if possible ...
 - Most of the time, function can follow some data definition template!
- Sometimes needed ...
 - E.g., to enforce compound invariants, without error
- Use helper predicate(s) to clearly describe invariant
 - E.g., “can-spend?”
 - No huge, unreadable boolean expressions!
- Function name and purpose stmt must indicate “**if**” usage!
 - E.g., “maybe-”
- 1 per function only
 - no nested “**if**”s!

Random

Ball Animation

Design a **big-bang** animation that:

- Start: a single ball, moving with **random x and y velocity**

Randomness

[bracketed args] = optional

`(random k [rand-gen])` → `exact-nonnegative-integer?`

`k` : `(integer-in 1 4294967087)`

`rand-gen` : `pseudo-random-generator?`

= `(current-pseudo-random-generator)`

When called with an integer argument *k*, returns a random exact integer in the range 0 to *k*-1.

Optional arg Default value

`(random min max [rand-gen])` → `exact-integer?`

`min` : `exact-integer?`

`max` : `(integer-in (+ 1 min) (+ 4294967087 min))`

`rand-gen` : `pseudo-random-generator?`

= `(current-pseudo-random-generator)`

When called with two integer arguments *min* and *max*, returns a random exact integer in the range *min* to *max*-1.

“random” is not random???

A pseudorandom number generator (PRNG), also known as a **deterministic random bit generator (DRBG)**,^[1] is an algorithm for generating a sequence of numbers whose properties approximate the properties of sequences of random numbers. The PRNG-generated sequence is not truly random, because it is completely determined by an initial value, called the PRNG's *seed*

Not secure!
e.g., for generating passwords

VS

A **cryptographically secure** pseudorandom number generator (CSPRNG) or cryptographic pseudorandom number generator (CPRNG) is a pseudorandom number generator (PRNG) with properties that make it suitable for use in cryptography.

Random Functions: Same Recipe (almost)!

```
;; A Velocity is a non-negative integer  
;; Interp: reresents pixels/tick change in a ball coordinate  
(define MAX-VELOCITY 10)
```

```
;; random-velocity : -> Velocity  
;; returns a random velocity between 0 and MAX-VELOCITY  
(define (random-velocity)  
  (random MAX-VELOCITY))
```

Functions can
have zero args

Random functions have
no examples

```
(check-true (< (random-velocity) MAX-VELOCITY))  
(check-true (>= (random-velocity) 0))  
(check-true (integer? (random-velocity)))  
(check-pred (λ (v) (and (integer? v)  
                        (< v MAX-VELOCITY)  
                        (>= v 0))))  
  (random-velocity))
```

Can still **test!**
Just less precise

```
;; random-x      : -> ???  
;; random-y      : -> ???  
;; random-ball   : -> ???
```