

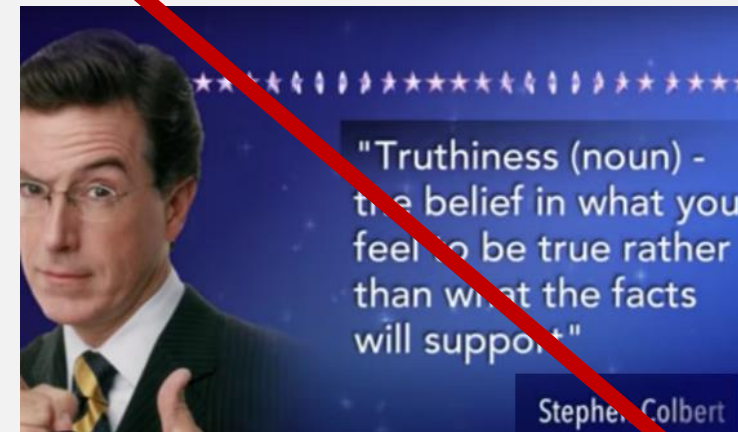
UMass Boston Computer Science
CS450 High Level Languages

Type Conversions, “Truthiness”

Tuesday, April 7, 2026

Logistics

- HW 8 in
 - ~~due: Tues 4/7, 11am EST~~
- HW 9 out
 - due: Tues 4/14, 11am EST



See also: [Implicit type conversion](#)

In some programming languages, any [expression](#) can be evaluated in a context that expects a [Boolean data type](#). Typically (though this varies by programming language) expressions like the number [zero](#), the [empty string](#), empty lists, and [null](#) are treated as false, and strings with content (like "abc"), other numbers, and objects evaluate to true. Sometimes these classes of expressions are called **falsy** and **truthy**. For example, in [Lisp](#), [nil](#), the empty list, is treated as false, and all other values are treated as true. In [C](#), the number 0 or 0.0 is false, and all other values are treated as true.



In [JavaScript](#), the empty string (`""`), `null`, `undefined`, `NaN`, `+0`, `-0` and `false`^[3] are sometimes called *falsy* (of which the [complement](#) is *truthy*) to distinguish between strictly [type-checked](#) and [coerced](#) Booleans (see also: [JavaScript syntax#Type conversion](#)).^[4] As opposed to Python, empty containers (arrays, maps, sets) are considered truthy. Languages such as [PHP](#) also use this approach.

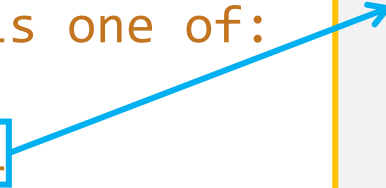
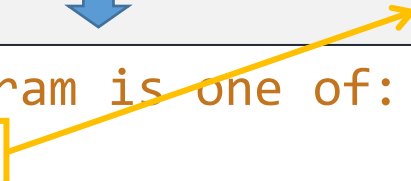
“CS450 LANG”

Programmer writes:

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

```
;; An Atom is one of:  
;; - Number  
;; - 450Bool
```

```
;; A 450Bool is either:  
;; - '450true  
;; - '450false
```



“CS450 LANG”

Programmer writes:



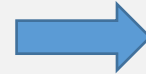
```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```



“eval450”

```
;; A Result is one of:  
;; - Number  
;; - Boolean
```

parse



```
;; An AST is one of:  
;; - (mk-num Number)  
;; - (mk-boo Boolean)  
;; - (mk-add AST AST)  
;; - (mk-mul AST AST)
```

```
(struct num AST [val])  
(struct boo AST [val])  
(struct add AST [lft rgt])  
(struct mul AST [lft rgt])
```



run

(following JS semantics?)

“CS450 LANG” Examples

Programmer writes:



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

Valid Program?



“eval450”

```
;; A Result is one of:  
;; - Number  
;; - Boolean
```

```
(check-equal? (eval450 100) 100)
```

```
(check-equal? (eval450 '450true) #t)
```

```
(check-equal? (eval450 '(+ 100 200)) 300)
```

```
(check-equal? (eval450 '(+ 450true 450)) 451)
```

```
(check-equal? (eval450 '(+ 1 2 3 4)) ??? )
```

```
match: no matching clause for '(+ 1 2 3 4)
```

Dynamic Errors (e.g, Exceptions)

When a function argument:

1. Comes from arbitrary users
2. Has a sufficiently complex data definition
 - So that contracts are not enough to enforce the signature
 - (Typically involves recursive data)

Then **dynamic errors** may be needed

Parsing: “CS450 LANG” Programs

```
;; parse: Program -> AST  
;; Converts a CS450 Lang surface program to its AST
```

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

```
(define (Program? p)  
  (or (atom? p)  
      (cons? p)))
```

The best (shallow check) we can do

```
(define/contract (parse p)  
  (-> Program? AST?)  
  (match p  
    [(? atom?) (parse-atom p)]  
    [`(+ ,x ,y) (mk-add (parse x) (parse y))]  
    [`(× ,x ,y) (mk-mul (parse x) (parse y))]))
```

function argument:

1. Comes from arbitrary users
2. Has sufficiently complex data definition where contracts are insufficient

Parsing: “CS450 LANG” Programs

```
;; parse: Program -> AST  
;; Converts a CS450 Lang surface program to its AST
```

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

```
(define/contract (parse p)  
  (-> Program? AST?)  
  (match p  
    [(? atom?) (parse-atom p)]  
    [`(+ ,x ,y) (mk-add (parse x) (parse y))]  
    [`(× ,x ,y) (mk-mul (parse x) (parse y))]  
    [_ (error ... )]))
```

function argument:

1. Comes from arbitrary users
2. Has sufficiently complex data definition where contracts are insufficient

Interlude: Racket exceptions

Exceptions are just special structs

Super struct (enables using exception API)

```
(struct exn:fail:syntax:cs450 exn:fail:syntax [])
```

```
(define/contract (parse p)
  (-> Program? AST?)
  (match p
    [(? atom?) (parse-atom p)]
    [ `( + ,x ,y) (mk-add (parse x) (parse y))]
    [ `( × ,x ,y) (mk-mul (parse x) (parse y))]
    [ _ (error ... )]))
```

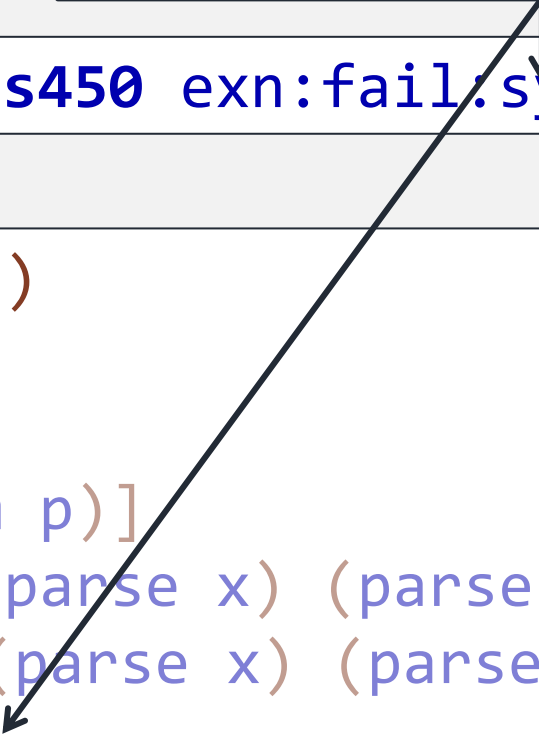
Interlude: Racket exceptions

Exceptions are just special structs

Super struct (enables using exception API)

```
(struct exn:fail:syntax:cs450 exn:fail:syntax [])
```

```
(define/contract (parse p)
  (-> Program? AST?)
  (match p
    [(? atom?) (parse-atom p)]
    [`(+ ,x ,y) (mk-add (parse x) (parse y))]
    [`(× ,x ,y) (mk-mul (parse x) (parse y))]
    [_ (raise-syntax-error
        'parse "not a valid CS450 Lang program" p
        #:exn exn:fail:syntax:cs450))]))
```



“CS450 LANG” Invalid Syntax Example

Programmer writes:



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```



“eval450”

```
;; A Result is one of:  
;; - Number  
;; - Boolean
```

```
(check-equal? (eval450 '(+ 1 2 3 4)) ??? )
```

```
match: no matching clause for '(+ 1 2 3 4)
```

```
parse: not a valid CS450 Lang program in: (+ 1 2 3 4)
```

Can write tests with exceptions!

```
(check-exn exn:fail:syntax:cs450?  
  (λ () (eval450 '(+ 1 2 3 4))))
```

Interlude: Racket exceptions (low-level) alternative

```
(struct exn:fail:syntax:cs450 exn:fail:syntax [])
```

```
(define/contract (parse p)
  (-> Program? AST?)
  (match p
    [(? atom?) (parse-atom p)]
    [`(+ ,x ,y) (mk-add (parse x) (parse y))]
    [`(× ,x ,y) (mk-mul (parse x) (parse y))]
    [_ (raise "low-level" raise
              (exn:fail:syntax:cs450
               (format "not a valid CS450 Lang program ~a" p)
               (current-continuation-marks))))]))
```

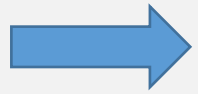
format is like "printf" that makes a string

"printf" format specifier (see also ~s ~v)

Stack Context of the exn

HW9

- Add another data type



- Strings

Supporting CS450 LANG String Programs

Programmer writes:



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

```
;; An Atom is one of:  
;; - Number  
;; - 450Bool  
;; - String
```

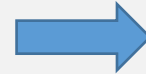
Supporting CS450 LANG String Programs

Programmer writes:



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```

parse



```
;; An AST is one of:  
;; ...  
;; - (mk-str String)  
;; ...  
  
;; ...  
  
(struct str AST [val])
```

Parsing “CS450 LANG + STRINGS” Programs

```
;; parse: Program -> AST  
;; Converts a 450Lang Program to AST
```

```
(define (parse p)  
  (match p  
    ...  
    [(? string?) (mk-str p)]  
    ...))
```

```
;; An AST is one of:  
;; ...  
;; -> (mk-str String)  
;; ...
```

```
;; ...
```

```
(struct str AST [val])
```

Running “CS450 Lang + Strings” Programs

```
;; run: AST -> Result  
;; computes the result of given program AST
```

```
;; A Result is a:  
;; - ...  
;; - String
```

```
;; An AST is one of:  
;; ...  
;; - (mk-str String)  
;; ...  
;; ...
```

```
(define (run p)  
  (match p  
    [(num n) n]  
    [(str s) s]  
    [(add x y) (???? (run x) (run y))]  
    [(mul x y) (???? (run x) (run y))])  
  (struct str AST [val]))
```

Running “CS450 Lang + Strings” Programs

```
;; run: AST -> Result  
;; computes the result of given program AST
```

```
;; A Result is a:  
;; - Number  
;; - String
```

What should happen when two strings are added???

e.g., What is the “meaning” of (+ “hello” “world!”)

```
(define (run p)  
  (match p  
    [(num n) n]  
    [(str s) s]  
    [(add x y) (450+ (run x) (run y))]  
    [(mul x y) (???? (run x) (run y))])
```

Last Time

```
;; 450+: Result Result -> Result  
;; “adds” two CS450Lang Result values together  
;; (following js semantics)
```

```
(define (450+ x y)  
  (+ (res->num x) (res->num y)))
```

```
;; A Result is a:  
;; - Number  
;; - Boolean
```


```
;; res->num: Result -> Number  
(define (res->num x)  
  (cond  
    [(number? x) ... ]  
    [(boolean? x) ... ]))
```

TEMPLATE

Last Time

```
;; 450+: Result Result -> Result  
;; “adds” two CS450Lang Result values together  
;; (following js semantics)
```

```
(define (450+ x y)  
  (+ (res->num x) (res->num y)))
```



```
;; res->num: Result -> Number  
(define (res->num x)  
  (cond  
    [(number? x) x]  
    [(boolean? x) (boo->num x)]))
```

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (+ (res->num x) (res->num y)))
```

```
;; A Result is a:
;; - Number
;; - Boolean
;; - String
```

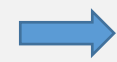
```
;; res->num: Result -> Number
(define (res->num x)
  (cond
    [(number? x) x]
    [(boolean? x) (boo->num x)]
    [(string? x) ??? (str->num x) ???]))
```

JavaScript Examples Exploration (3 min)

- repljs.com
 - “plus”
 - and “times”
 - with all different combinations of data types

```
;; A Result is a:  
;; - Number  
;; - Boolean  
;; - String
```

e.g., What is the “meaning” of (+ “hello” “world!”)



“helloworld!”

```
;; 450+: Result Result -> Result  
;; “adds” two CS450Lang Result values together  
;; (following js semantics)
```

```
(define (450+ x y)  
  (cond  
    [(and (number? x) (number? y)) (+ x y)]  
    ...  
    [(and (string? x) (string? y)) ???])
```

res->num is not enough!

+ is sometimes a string operation!

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(and (number? x) (number? y)) (+ x y)]
    ...
    [(and (string? x) (string? y)) (string-append x y)]
```

res->num is not enough!

+ is sometimes a string operation!

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(and (number? x) (number? y)) (+ x y)]
    [(string? y) ??? ]

    [(and (string? x) (string? y)) (string-append x y)]
```

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(and (number? x) (number? y)) (+ x y)]
    [(string? y) (string-append (?? x) y)]

    [(and (string? x) (string? y)) (string-append x y)]
```

Check if Bool behavior correct?
(TODO!)

```
;; A Result is a:  
;; - Number  
;; - Boolean  
;; - String
```

```
;; 450+: Result Result -> Result  
;; “adds” two CS450Lang Result values together  
;; (following js semantics)
```

```
(define (450+ x y)  
  (cond  
    [(and (number? x) (number? y)) (+ x y)]  
    [(string? y) (string-append (res->str x) y)]  
  
    [(and (string? x) (string? y)) (string-append x y)]
```

```
;; res->str: Result -> String  
(define (res->str x)  
  (cond  
    [(number? x) (num->str x)]  
    [(boolean? x) (boo->str x)]  
    [(string? x) x]))
```

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(and (number? x) (number? y)) (+ x y)]
    [(string? y) (string-append (res->str x) y)]
    [(string? x) (string-append x (res->str y))]
    [(and (string? x) (string? y)) (string-append x y)]
```

(can any cond clauses be combined?)

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(or (string? x) (string? y))
     (string-append (res->str x) (res->str y))]
    [else (+ x y)]))
```

Does this cover bools??
(TODO!)

```
;; 450+: Result Result -> Result
;; “adds” two CS450Lang Result values together
;; (following js semantics)
```

```
(define (450+ x y)
  (cond
    [(or (string? x) (string? y))
     (string-append (res->str x) (res->str y))]
    [else (+ (res->num x) ??? (res->num y))]))
```

Does this cover bools??
(TODO!)

Running: “CS450 LANG” Programs: “times”

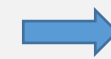
```
;; 450times: Result Result -> Result  
;; “multiplies” 450Lang Results  
;; (following js semantics)
```

```
(define (450times x y)  
  (cond  
    [(and (number? x) (number? y)) (* x y)]  
    [(and (number? x) (string? y)) ... ]  
    [(and (string? x) (number? y)) ... ]  
    [(and (string? x) (string? y)) ... ])))
```

JS Semantics Exploration: “times” strings

Not always the same as “plus”!

e.g., What is the “meaning” of (\times “hello” “world!”)



NaN ???

“Not a Number”

☰ NaN

From Wikipedia, the free encyclopedia

In [computing](#), **NaN** ([/næn/](#)), standing for **Not a Number**, is a particular [value](#) of a numeric [data type](#) (often a [floating-point number](#)) which is undefined or unrepresentable, such as the result of [0/0](#). Systematic use of NaNs was introduced by the [IEEE 754](#) floating-point standard in 1985, along with the representation of other non-finite quantities such as [infinities](#).

 mdn web docs 

NaN

The `NaN` global property is a value representing Not-A-Number.

Running: “CS450 LANG” Programs

```
;; run: AST -> Result  
;; computes the result of running a CS450Lang program AST
```

```
;; An AST is one of:  
;; - (num Number)  
;; - (boo Boolean)  
;; - (str String)  
;; - (add AST AST)  
;; - (mul AST AST)
```



```
;; A Result is either:  
;; - Number  
;; - Boolean  
;; - String
```

Running: “CS450 LANG” Programs – with NaN!

```
;; run: AST -> Result  
;; computes the result of running a CS450Lang program AST
```

```
;; An AST is one of:  
;; - (num Number)  
;; - (boo Boolean)  
;; - (str String)  
;; - (add AST AST)  
;;
```

Don't forget to update all “Result” functions!

```
;; res->str: Result -> String  
(define (res->str x)  
  (cond  
    [(string? x) x]  
    [(boolean? x) (bool->str x)]  
    [(number? x) (num->str x)]  
    [(NaN? x) “NaN”]))
```



```
;; A Result is either:  
;; - Number  
;; - Boolean  
;; - String  
;; - NaN  
(struct nan [])  
(define NaN (nan)) ; “singleton”
```

Predicate? (TODO!)

Running: “CS450 LANG” Programs: “times”

```
;; 450times: Result Result -> Result  
;; “multiplies” two 450 lang Results  
;; (following js semantics)
```

```
(define (450times x y)      ???  
  (cond  
    [(and (number? x) (number? y)) (* x y)]  
    [else NaN]))
```

```
;; A Result is either:  
;; - Number  
;; - Boolean  
;; - String  
;; - NaN  
(struct nan [])  
(define NaN (nan))
```

Does this cover all corner cases?
Try: '(× “two” 4)

CS450Lang - Using Other Data Types

- **Need boolean constructs** (also follow JS semantics?):
 - “equality” (JS “loose” == vs “strict” === ?)
 - conditional (JS “truthy”?)



A new 450 LANG Boolean construct

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)
```



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)  
;; - `(iffy ,Program ,Program ,Program)
```

(sort of like "if")

Truthiness – more than Booleans

In [JavaScript](#), a **truthy** value is a value that is considered `true` when encountered in a [Boolean](#) context. All values are truthy unless they are defined as [falsy](#). That is, all values are *truthy* except `false`, `0`, `-0`, `0n`, `""`, `null`, `undefined`, `NaN`, and [document.all](#).

A new 450 LANG Boolean construct

```
;; js "truthy true"  
(check-equal? (eval450 '(iffy 10 100 200)) 100)  
;; js "truthy false"  
(check-equal? (eval450 '(iffy (- 100 100) "a" "b")) "b")
```

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)  
;; - `(iffy ,Program ,Program ,Program)
```

Truthy

Falsy

CS450Lang - Using Other Data Types

- **Need boolean constructs** (also follow JS semantics?):
 - “equality” (JS “loose” == vs “strict” === ?)
 - conditional (JS “truthy”?)

A 450 Lang “Equality” Operator

```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)  
;; - `(iffy ,Program ,Program ,Program)
```



```
;; A Program is one of:  
;; - Atom  
;; - `(+ ,Program ,Program)  
;; - `(× ,Program ,Program)  
;; - `(iffy ,Program ,Program ,Program)  
;; - `(≈ ,Program ,Program)
```

A “Loose” Equality Operator

- Follow JS == “loose” equality operator (look it up)

Double equals (==) will perform a type conversion when comparing two things,

```
const num = 0;  
const str = "0";  
console.log(num == str); // true
```

Is this right???

```
;; weird “loose” ~= test case  
(check-true (eval450 '(~= (+ 10 90) (+ "10" "0")))))
```

```
;; A Program is one of:  
;; - Atom  
;; - `( + ,Program ,Program )  
;; - `( × ,Program ,Program )  
;; - `( iffy ,Program ,Program ,Program )  
;; - `( ~= ,Program ,Program )
```

As language designers,
we give the meaning to
these symbols